

Multiscale Modeling of CO₂ Flow and Storage in Pre-Salt Reservoirs: Perspectives and Challenges

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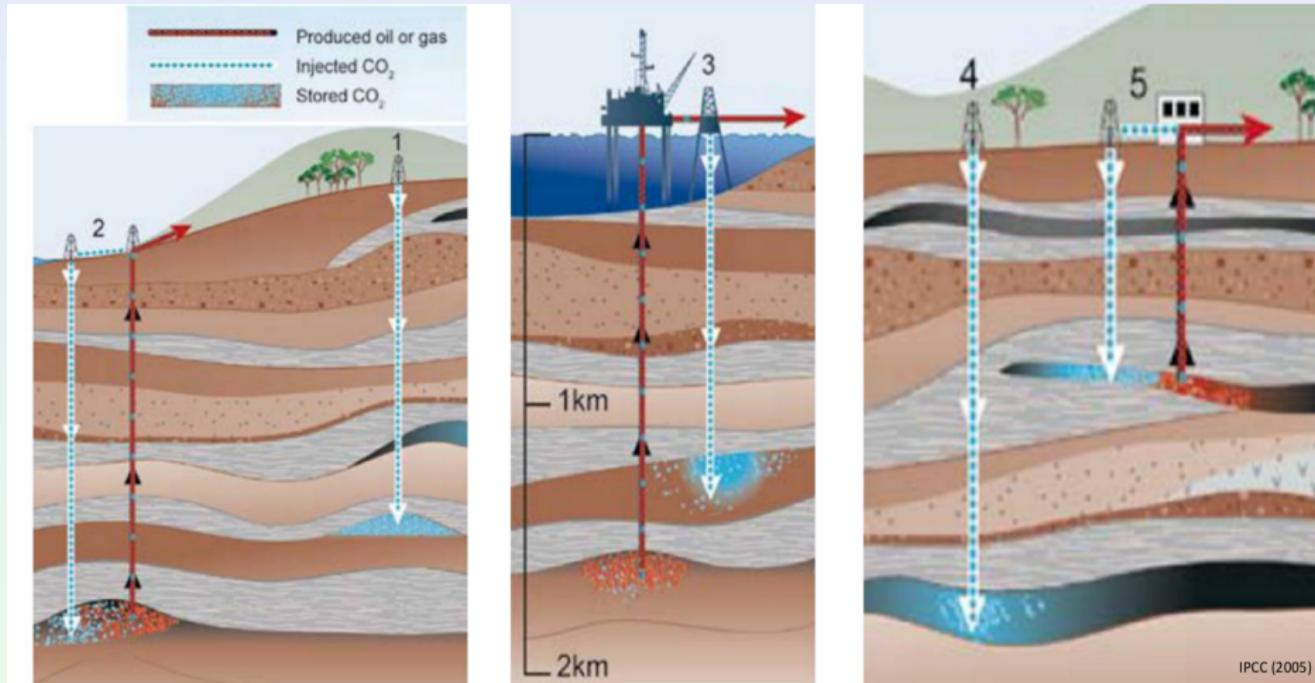
—

and
Marcio Murad
LNCC/MCTIC



OUR MAIN TARGET

Feasibility of Vuggy Carbonates (Pre-Salt) as Potential Storage Sites for CO₂ Storage



➤ Oil fields

- 1- Depleted reservoirs (gas/oil)
- 2- Enhanced oil recovery

ABC

➤ Saline Aquifers;

- 3- Deep unused saline water-saturated reservoir rocks.

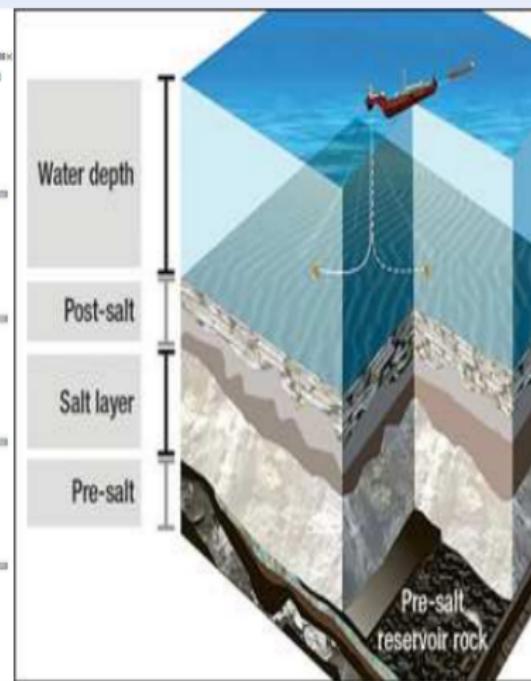
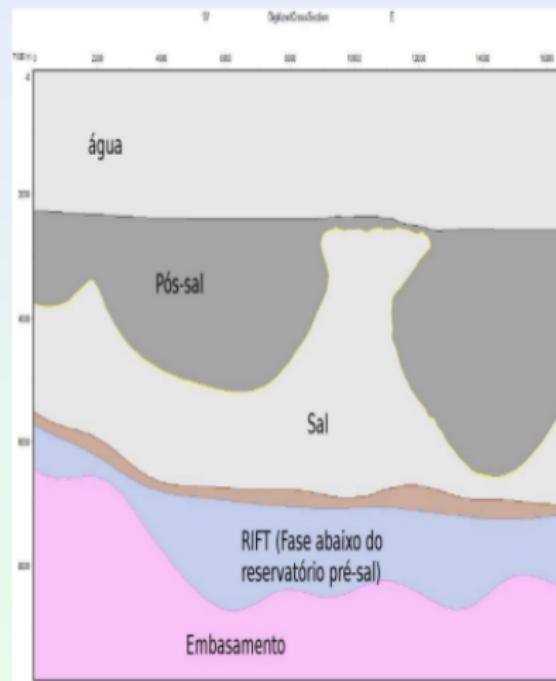
COMOHR/LNCC

➤ Coal layers.

- 4- Deep Unmineable coal
- 5- ECBM Recovery

Possible Choices for Storage Sites

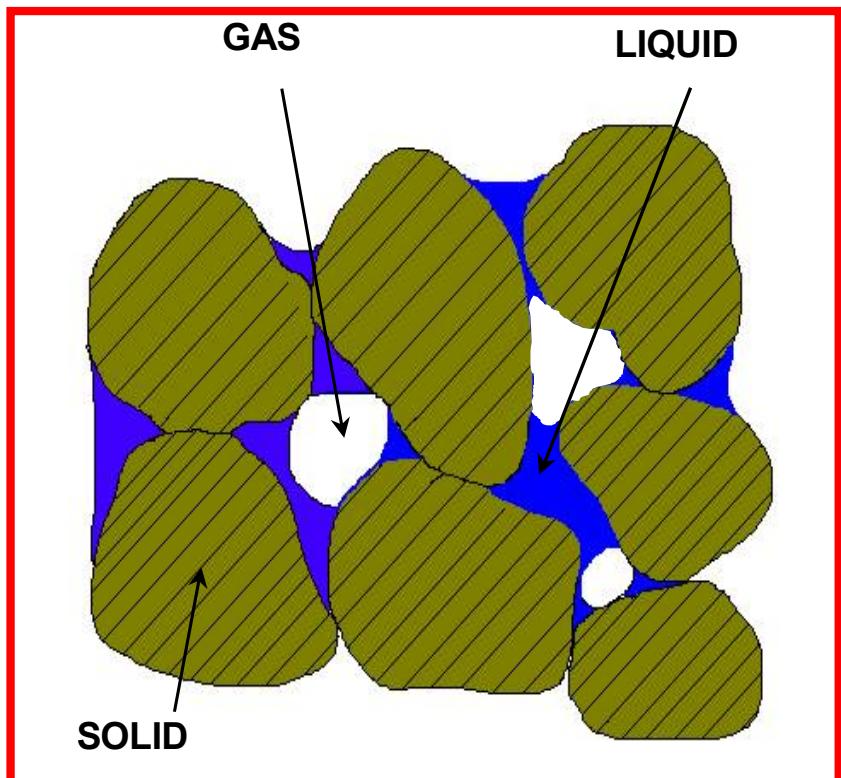
Carbonate Underneath the Salt Layer or Rock Salt



OUTLINE OF THE LECTURE

- Pros and Cons
 - Storage Site: Carbonate underneath the Salt Layer
 - Review of CO_2 -properties at the Subsurface
 - CO_2 movement and Driving Forces
 - Thermodynamics
 - Geochemistry
 - Review of the Main Trapping Mechanisms in the Subsurface
 - Stratigraphic, Residual,
 - Solubility, Mineral
 - Drawbacks: (Ongoing Research)
 - Geomechanical Issues
 - Appearance of High Permeability Pathways - Conduits
 - Storage Site: Salt Layer
- Concluding Remarks on Feasibility of CO_2 Storage in the Pre-Salt

Multiphase multispecies approach



The **species** are:

- mineral (-) : main mineral
- water (w) : as liquid or evaporated in the gas phase
- air (a) : dry air, as gas or dissolved in the liquid phase
- chemical species : interacting (reactive) species

The **three phases** are:

- gas (g) : mixture of dry air and water vapour
- liquid (l) : water + air dissolved + dissolved chemical species
- solid (s) : main mineral + absorbed cations + precipitated minerals

Reactive transport equations

$$\frac{\partial}{\partial t}(\phi S_w \rho_w c_i) + \nabla \cdot \mathbf{j}_i = R_i \quad (i = 1, \dots, N)$$

Total Flow:

Chemical reactions

$$\mathbf{j}_i = \rho_w c_i \mathbf{q}_w + \mathbf{D}_w \nabla c_i + \phi S_w \rho_w c_i \dot{\mathbf{u}}$$

Advective

Non-advective
(dispersion and
diffusion)

Solid velocity

Reactive transport equations

$$\frac{\partial}{\partial t} (\phi S_w \rho_w c_i) + \nabla \cdot \mathbf{j}_i = R_i \quad (i = 1, \dots, N)$$

□ CHEMICAL INTERACTION OF N INTERACTING SPECIES

- Slow reactions: kinetics controlled
- Fast reactions: equilibrium controlled

□ PHENOMENA CONSIDERED

- Homogeneous reactions
 - Aqueous complex formation
 - Acid/base reactions
 - Oxidation/reduction reactions
- Heterogeneous reactions
 - Cation exchange
 - Dissolution/precipitation of minerals (equilibrium and kinetics)
- Other reactions
 - Radioactive decay
 - Linear sorption

Reactive transport equations

$$\frac{\partial}{\partial t} (\phi S_l \rho_l c_i) + \nabla \cdot \mathbf{j}_i = R_i \quad (i = 1, \dots, N)$$

□ CHEMICAL INTERACTION OF N INTERACTING SPECIES

□ Slow reactions: kinetics controlled

- Rate of species production in kinetics-controlled reactions

$$r_m = A_m k_m \left| \Omega_p^r - 1 \right|^n$$

$$\Omega_p = \frac{Q_m}{K_m} \quad ; \quad Q_m = \prod_{j=1}^{N_c} a_j^{v_{mj}}$$

$$k_m = k_{25} \exp \left[\frac{-E_a}{R} \left(\frac{1}{T} - \frac{1}{298.15} \right) \right]$$

□ Fast reactions: equilibrium controlled

- A chemical equilibrium model is used based on the minimization of Gibbs free energy

$$\underset{n_j^c, n_i^x}{\text{minimize}} \quad G = \sum_{j=1}^{N_c} \mu_j^c n_j^c + \sum_{i=1}^{N_x} \mu_i^x n_i^x$$

$$n_j^U = n_j^c + \sum_{i=1}^{N_x} v_{ij} n_i^x \quad (j = 1, \dots, N_c)$$

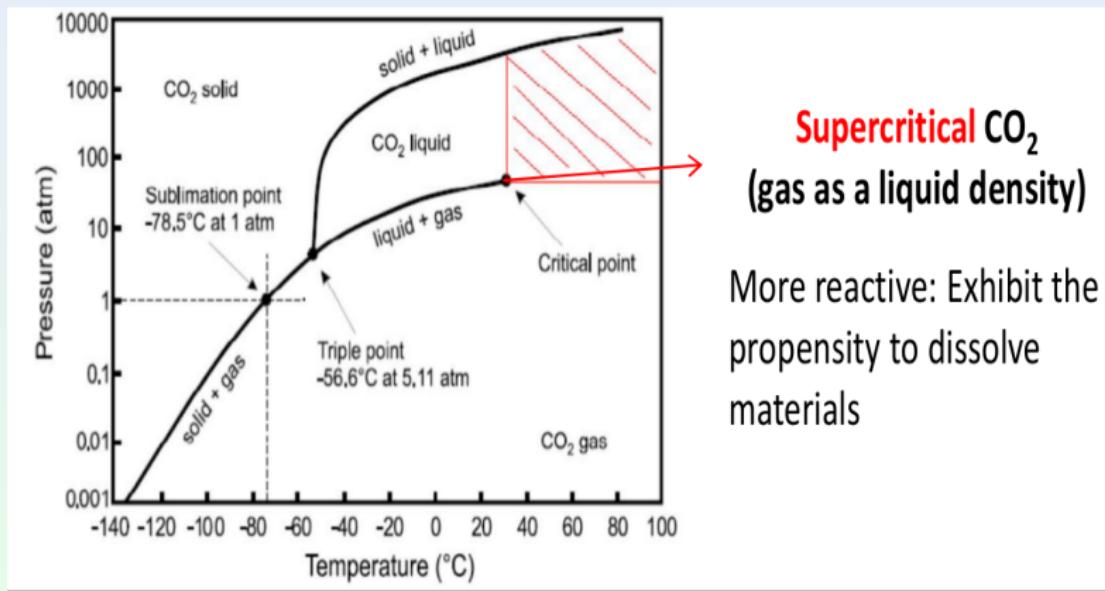
$$n_i^x \geq 0 \quad (i = 1, \dots, N_x)$$

$$n_j^c \geq 0 \quad (j = 1, \dots, N_c)$$

- Newton-Raphson algorithm
- Lagrange multipliers to incorporate the restrictions of the system

Thermodynamics: Supercritical State

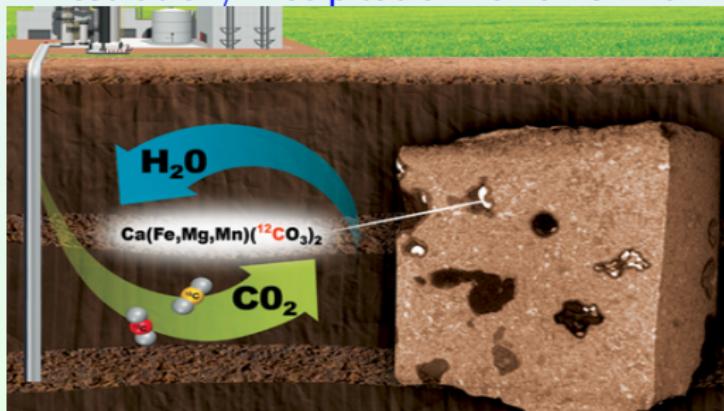
Temperature: 31.1°C , Pressure 7.38 MPa: Geothermal gradients $25^{\circ}/\text{KM}$, $z = 800\text{m}$.



- In the long-term behaves as a separate phase with much lower Volume

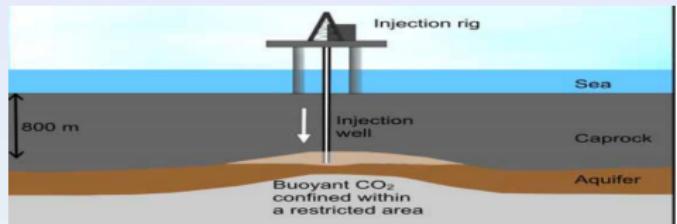
Desirable Properties for a Successful Injectivity

- Efficient Trapping Mechanics
- Host formation not impermeable
- Deep enough to maintain CO_2 in supercritical state
- High areal extent of the cap rock
- Avoidance of Geomechanical Structural Damage
- After Long Term Dissolution/Precipitation remains in a Mineralized state



Trapping Mechanics

i) Structural/stratigraphic Free Gas Phase



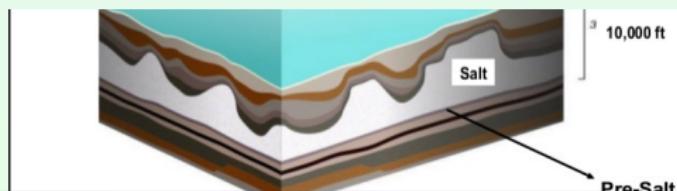
Two-Phase Flow in Porous Media. Buoyant Forces

$$\mathbf{v}_T = -KK_r(S)(\nabla P - \rho \mathbf{g})$$

$$\phi \frac{\partial S}{\partial t} + \nabla \cdot (\mathbf{v}_T f(S)) = 0$$

$$f = f_w(1 - \alpha(Kg(\rho_w - \rho_g)))$$

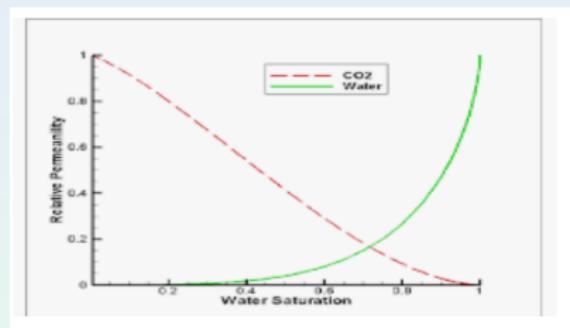
Salt (Halite and Dolomite) – Excellent non-reactive Impermeable Medium.



Trapping Mechanics

ii) Residual Trapping

Also referred to as capillary trapping



[Relative Permeability Curves

$$\mathbf{v}_T = -\frac{K}{\mu} K_r(S)(\nabla P - \rho \mathbf{g}), \quad \phi \frac{\partial S}{\partial t} + \nabla \cdot (\mathbf{v}_T f(s)) = 0$$

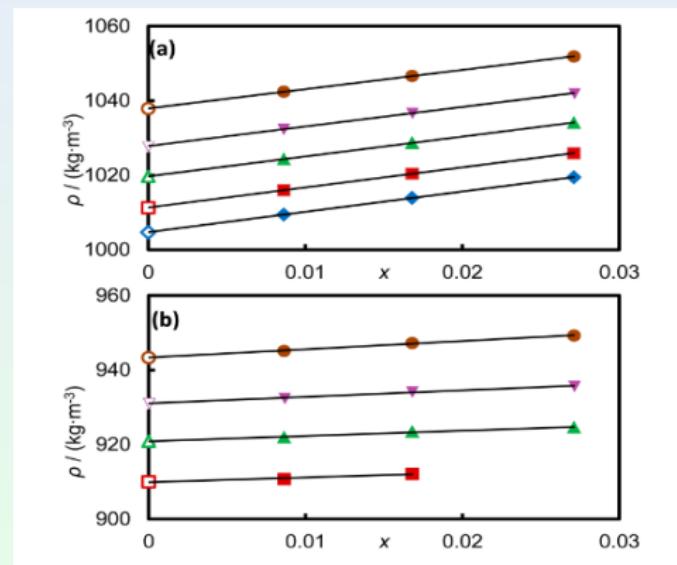
- A fraction of the CO₂ is left behind as a disconnected phase

Trapping Mechanics

iii) Solubility in the Aqueous Phase

Increase in Brine Density

$$\rho = \rho_{\text{water}}(1 - X) + X\rho_{CO_2}, \quad X = \text{mass fraction } C_{O_2}$$



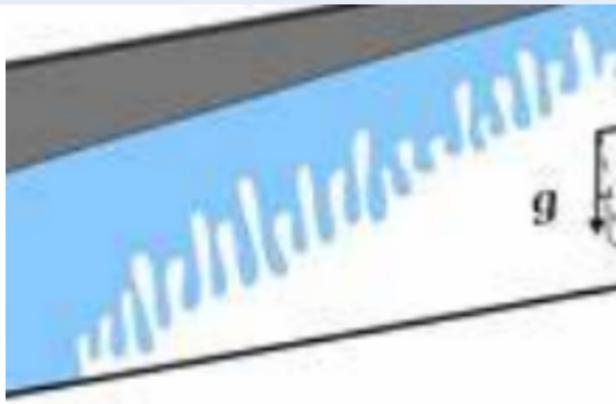
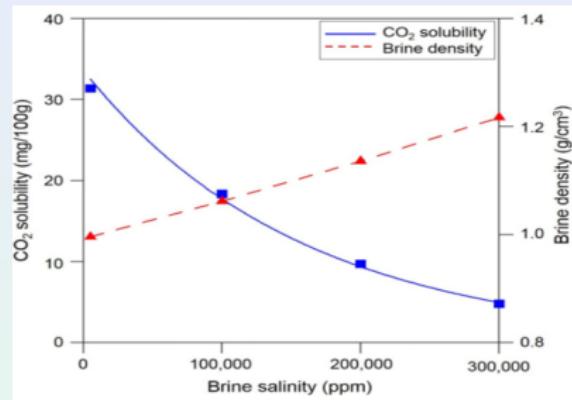
Top $T = 296 \text{ K}$:

Bottom $T = 449 \text{ K}$

Trapping Mechanics

iii) Solubility in the Aqueous Phase

Increase in Brine Density – Gravitational stability, $\rho_w = \rho_w(C_{CO_2})$



- Moves in the Opposite Direction of the Free Gas.
- Sinks towards the bottom of the host formation
- Mass fraction – Convective-Diffusion Reaction Equation

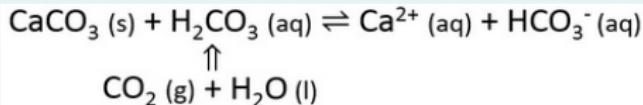
$$\phi \frac{\partial \phi(\rho_w X_i)}{\partial t} + \nabla \cdot (\rho_w X_i \mathbf{v}_D) = \nabla \cdot (D_i \nabla(\rho_w X_i)) + F_i, \quad i = CO_2, \text{water}$$

Trapping Mechanisms: iv) Mineral Trapping

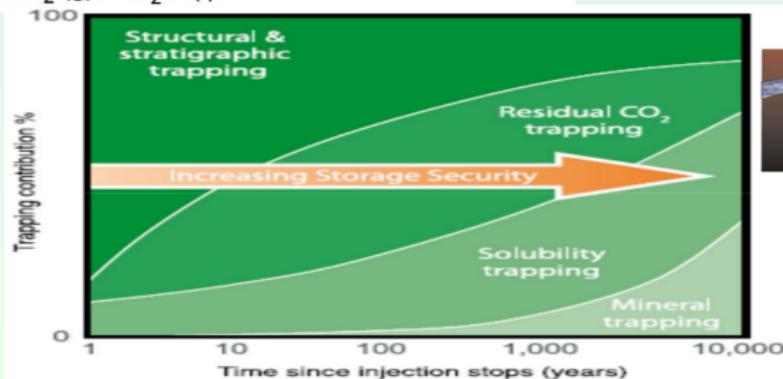
- Solubility → Acidification → Weak carbonic acid



- Trigger Dissolution – Precipitation Geochemical Reactions

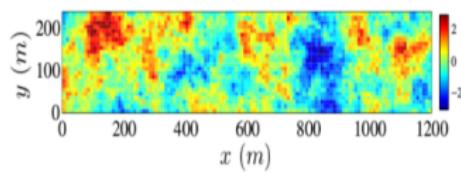
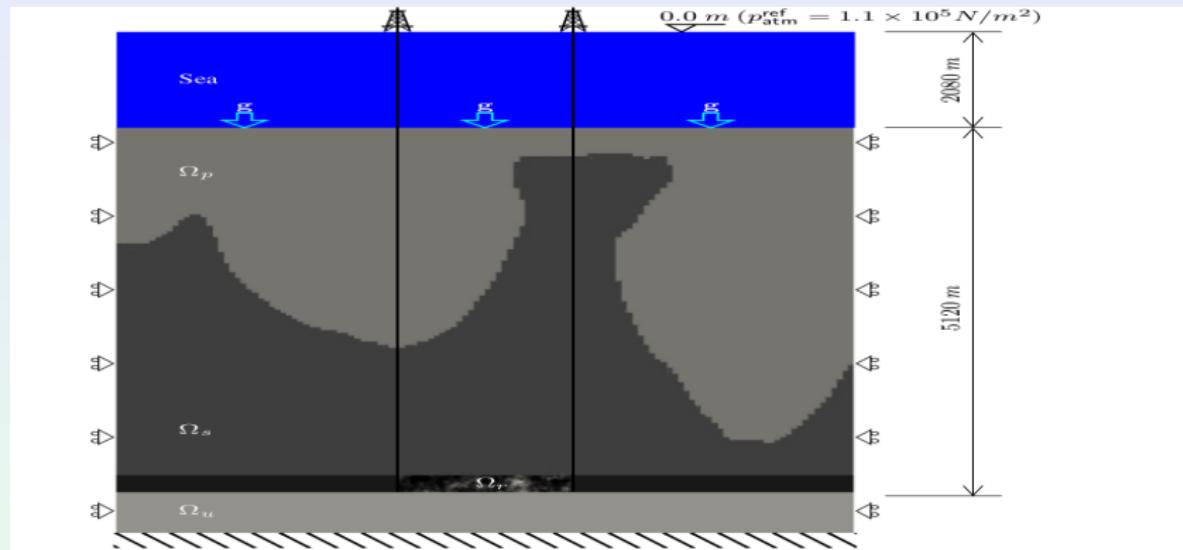


Time Scales

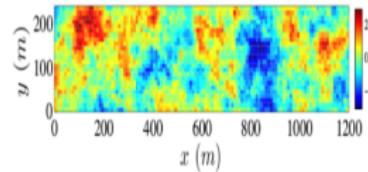


Drawbacks: Structural Geomechanics

i) Integrity of the Cap Rock



(b) Log-permeability



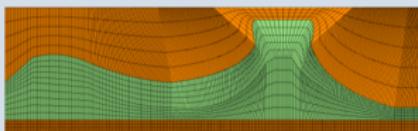
(a) Log-porosity

Hydro-Mechanical Multi-Physics Coupled Model

- Two-Phase Flow, Elasticity of the Host Rock,
- Viscoelasticity of the Cap Rock Salt

Fixed Stress Split: Creep of the Rock Salt)

$$\begin{aligned}\operatorname{div} \boldsymbol{\sigma}_e &= -\rho_s^{POS} \mathbf{g} \\ \boldsymbol{\sigma}_e &= \mathcal{C} \mathbb{E}_e + \boldsymbol{\sigma}^0 \quad \text{in } \Omega_{POS} \\ \mathbb{E}_e &= \frac{1}{2} (\nabla \mathbf{u} + (\nabla \mathbf{u})^T)\end{aligned}$$



$$\begin{aligned}\operatorname{div} \boldsymbol{\sigma}_e &= -\rho_s^{DOMO} \mathbf{g} \\ \boldsymbol{\sigma}_e &= \mathcal{C} \mathbb{E}_e + \boldsymbol{\sigma}^0 \\ \mathbb{E} &= \nabla^s \mathbf{u} \\ \mathbb{E}_e &= \mathbb{E} - \mathbb{E}_v \\ \mathbf{S} &= 2G \mathbf{P}_{dev} \mathbb{E}_e \quad \text{in } \Omega_{SALT} \\ \dot{\mathbb{E}}_v &= \dot{\gamma} \frac{\partial \sigma_v}{\partial \sigma} = \dot{\gamma} \sqrt{\frac{3}{2}} \frac{\mathbf{S}}{\|\mathbf{S}\|} \\ \dot{\gamma} &= \mathcal{E}_R^* \left(\frac{\sigma_v}{\sigma_R} \right)^N \quad \sigma_v = \sqrt{\frac{3}{2}} \|\mathbf{S}\|\end{aligned}$$

$$\operatorname{div} \boldsymbol{\sigma}_e = \nabla p - \left((S_w \rho_w + (1 - S_w) \rho_o) \phi + \rho_s^{RES} (1 - \phi) \right) \mathbf{g}$$

$$\boldsymbol{\sigma}_e = \mathcal{C} \mathbb{E}_e + \boldsymbol{\sigma}^0, \quad \mathbb{E}_e = \frac{1}{2} (\nabla \mathbf{u} + (\nabla \mathbf{u})^T)$$

$$\beta \frac{\partial p}{\partial t} + \operatorname{div} \mathbf{v}_{Dt} = -\beta \frac{\partial \tilde{\sigma}}{\partial t} \quad \text{in } \Omega_{RES}$$

$$\mathbf{v}_{Dt} = -\lambda_t (S_w) K(\phi) (\nabla p + \mathbb{E})$$

$$\frac{\partial (S_w \phi)}{\partial t} + \operatorname{div} (\lambda_w (S_w) (\mathbf{v}_{Dt} - \eta k_{ro})) = 0$$

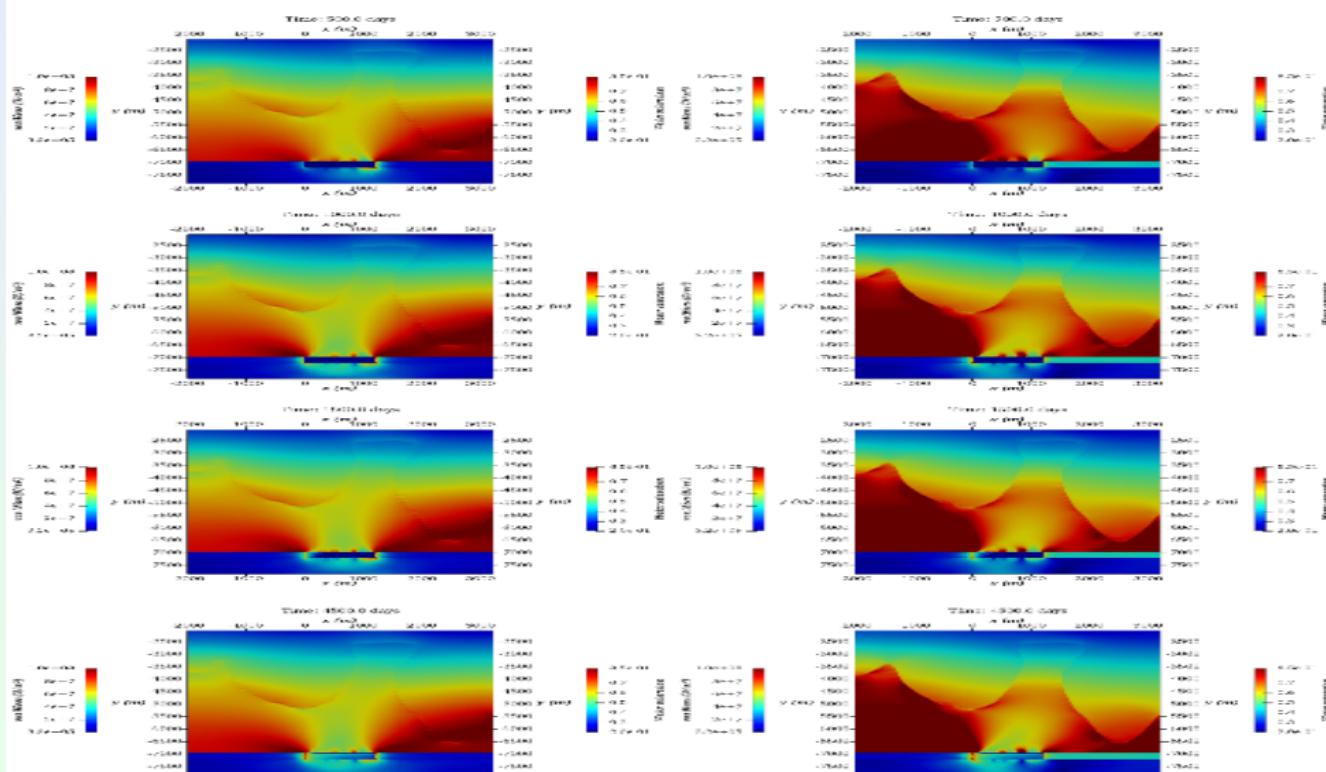
Saturation and Von-Mises Stress

Elastic

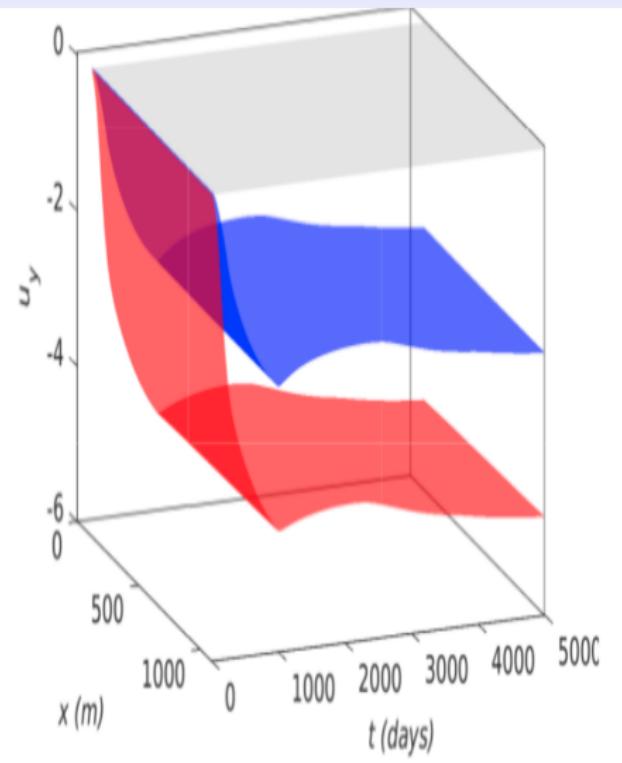
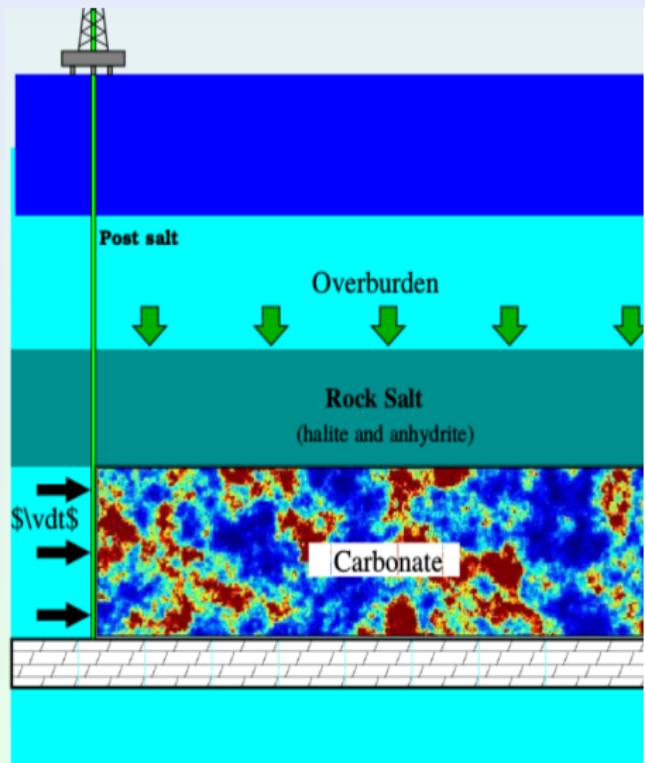
x

Viscoelastic

1.1 Elastic \times Viscoelastic



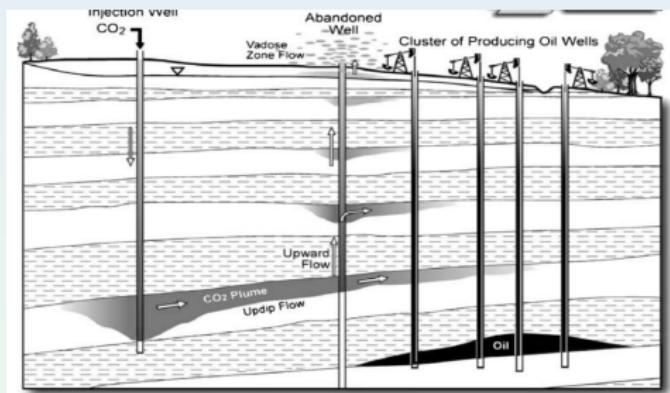
Surface Uplift



Structural Geomechanical Issues

ii) Leakage through Abandoned Wells

- Saline Aquifers; Do not suffer from this possibility
- Oil fields. Anthropogenic activity.



- Preexisting Abandoned wells penetrating caprock
- Potential leakage high-permeability pathways for buoyant CO_2

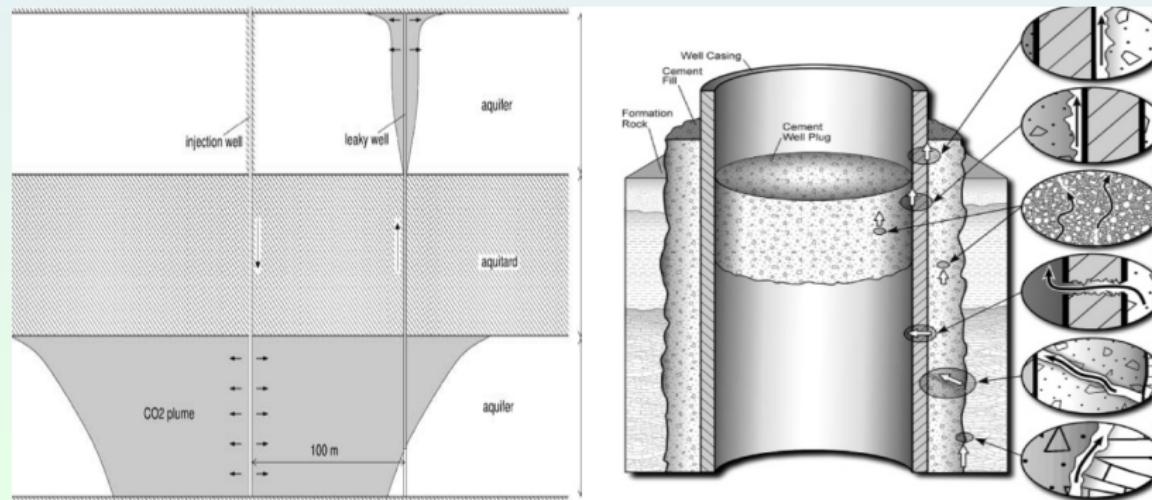
Structural Geomechanical Issues

ii) Leakage through Abandoned Wells

Two-Phase Flow (Celia et al 2013)

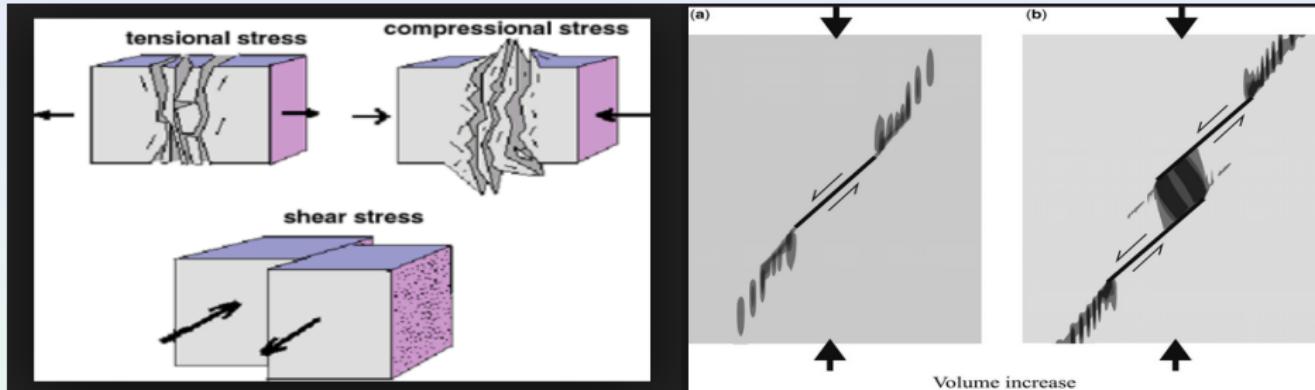
$$\phi \frac{\partial \rho_g S_g}{\partial t} - \nabla \cdot (\rho_g \lambda_g \mathbf{K}(\nabla P - \rho_g \mathbf{g})) = 0$$

$$\phi \frac{\partial S_w}{\partial t} - \nabla \cdot (\lambda_w \mathbf{K}(\nabla P - \rho_w \mathbf{g})) = 0$$

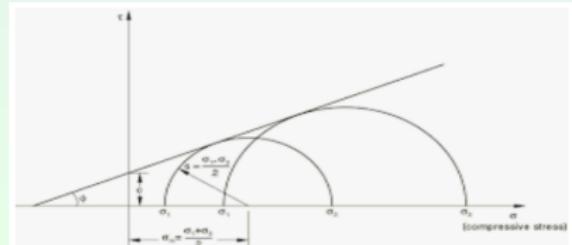


Structural Geomechanics

iii) Fault Activation due to Fluid Over-Pressurization



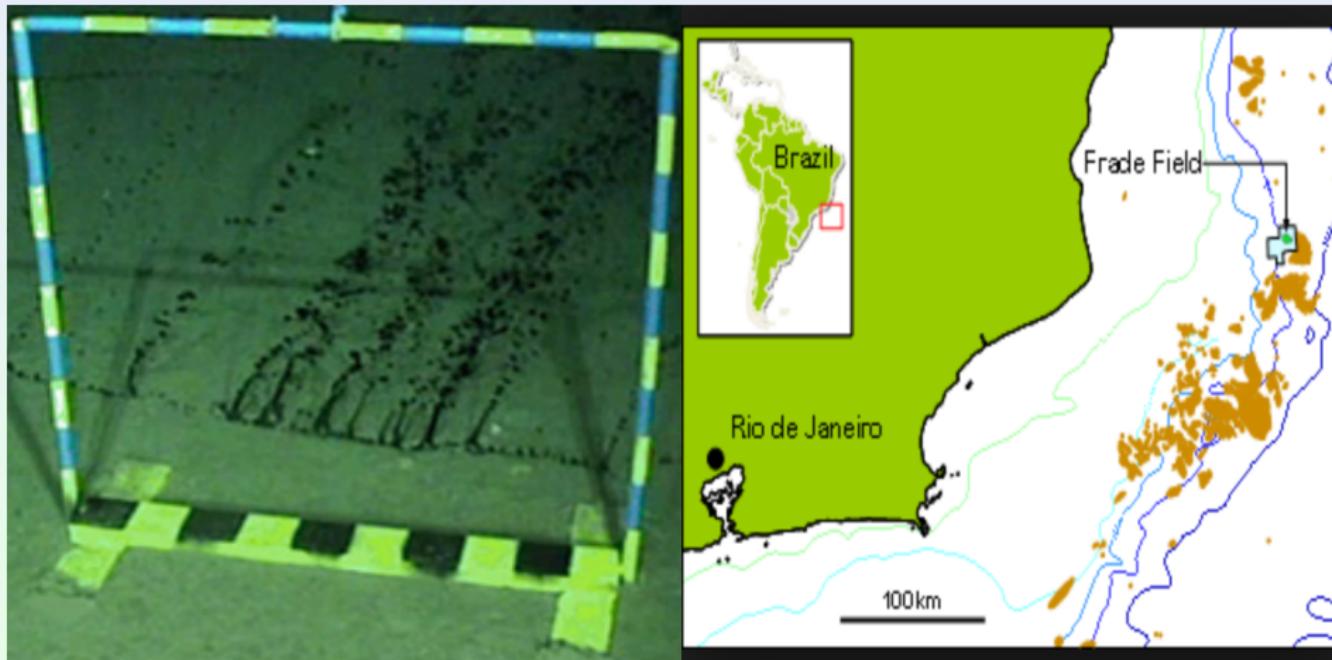
Localized Leaking: Plasticity. Mohr Coulomb Function. $\dot{\mathcal{E}}_p = \lambda \partial F(\sigma) / \partial \sigma$



Structural Geomechanics

iii) Fault Activation

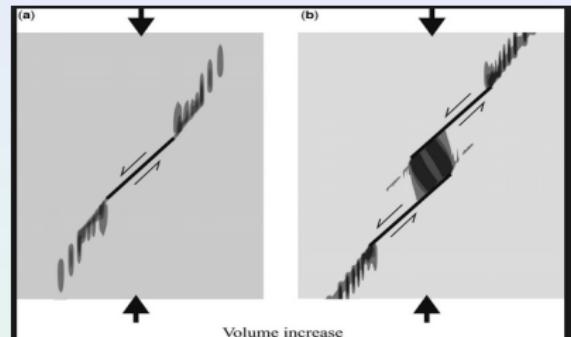
- Frade Field Oil Spill Incident



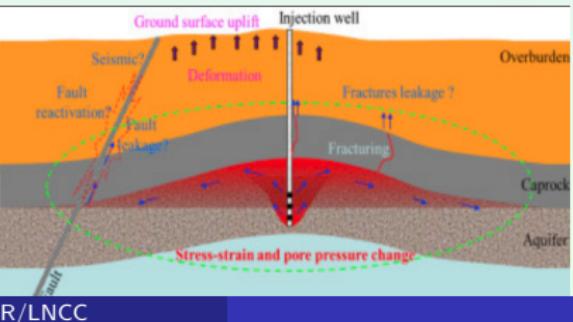
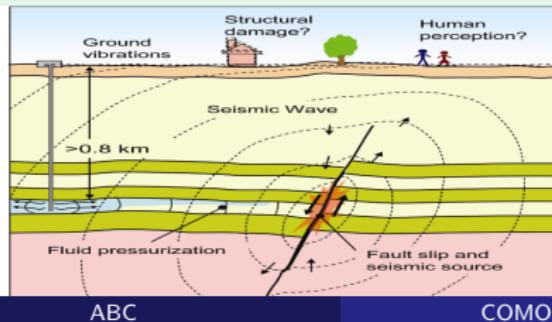
iii) Fault Activation

Dilatancy: Increase in Permeability

$$\frac{\partial \phi \rho_G}{\partial t} + \nabla \cdot (\rho_G \mathbf{v}_D) = 0, \quad \mathbf{v}_d = -K(\nabla p - \rho_G \mathbf{g})$$



Injection-Fault-Activation → Ground Surface Uplift and Induced Siesmicity



Structural Geomechanical

iv) Water Weakening. Loss of Injectivity

Injectivity Index

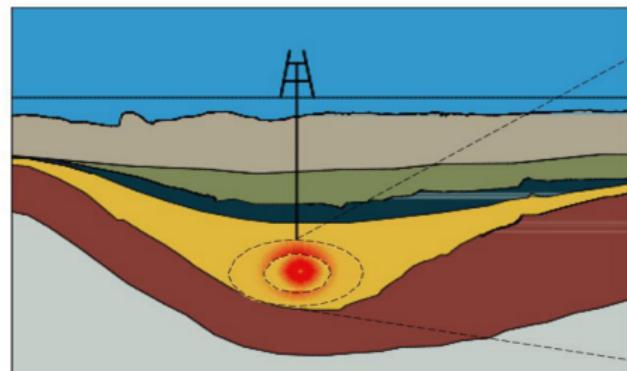
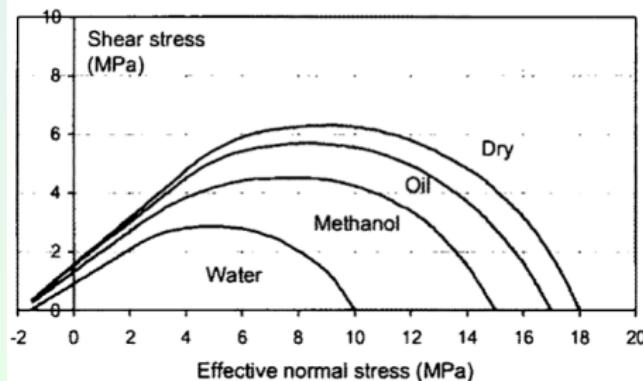
$$II = \frac{\text{Injection Flow Rate}}{P_{inj} - P_{res}}$$

Low pH triggers dissolution/precipitation reactions new the injector

Geomechanics: Poroplasticity: Decrease strength of the rock bonds.

$$\nabla \cdot \sigma - \nabla P = 0, \quad \sigma = C(\mathcal{E}(u) - \mathcal{E}_p)$$

$$\dot{\mathcal{E}}_p = \lambda \partial F(\sigma, S) / \partial \sigma$$

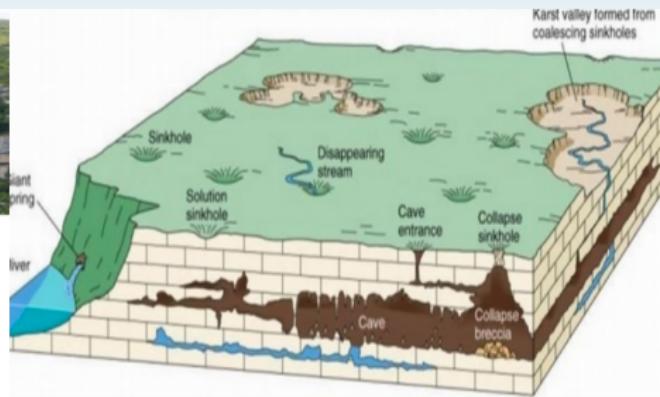


Presence of a Cave Network

Karst Conduits

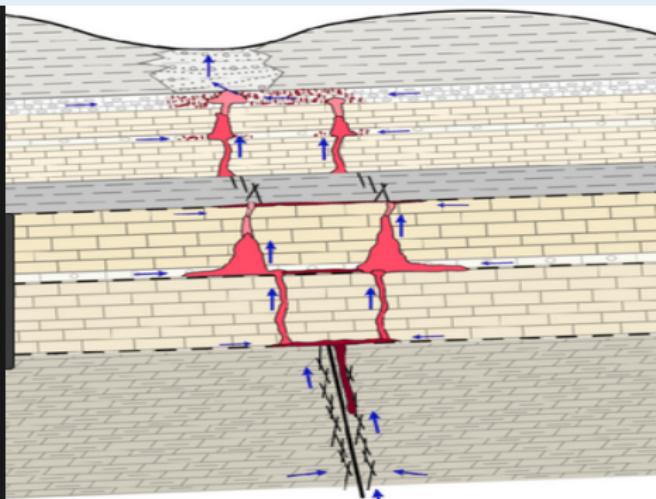
- Fractured Corridors. Enlarged due to Dissolution Collapse

Análogo
de
Rocha
Karstificada

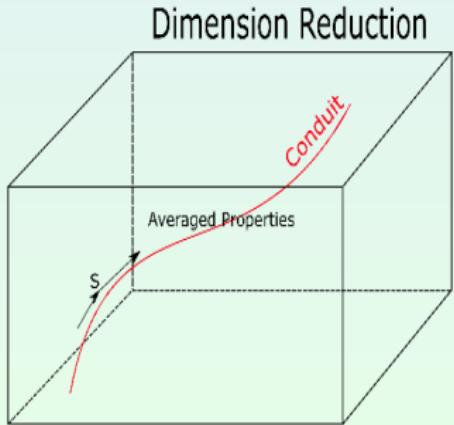
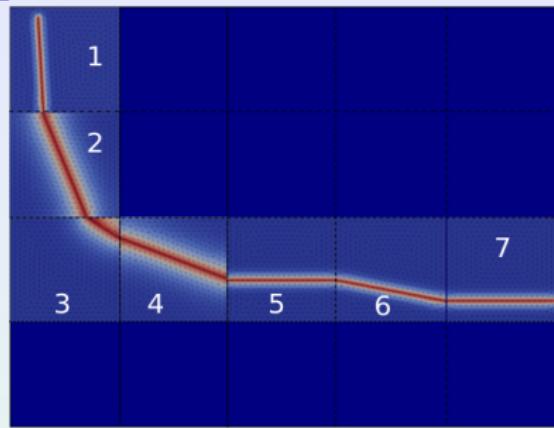


Presence of a Cave Network

Karst Conduits



Coupled 3D - 1D Model



$$\beta_r \frac{\partial P_r}{\partial t} + \nabla \cdot \mathbf{v}_d = KI(P_r - P_c)\delta_\Delta \quad \text{in } \Omega$$
$$\mathbf{v}_d = -K\nabla P_r$$

Coupled System

$$\beta_c \frac{\partial P_c}{\partial t} + \frac{dv_c}{ds} = -\frac{KI}{A_c}(P_r - P_c)$$

$$v_c = -K \frac{dp_c}{ds} \quad \text{in } \Gamma_c$$

Summary - High-Fidelity (Fine-Scale) Model

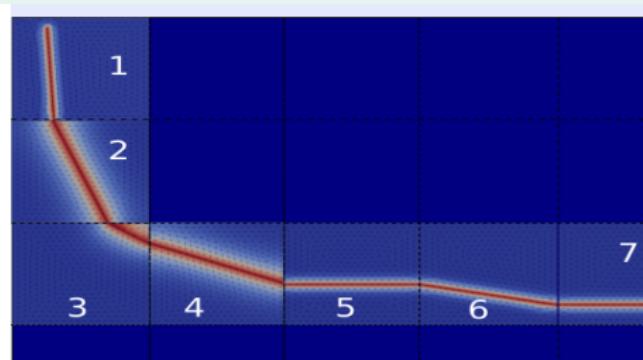
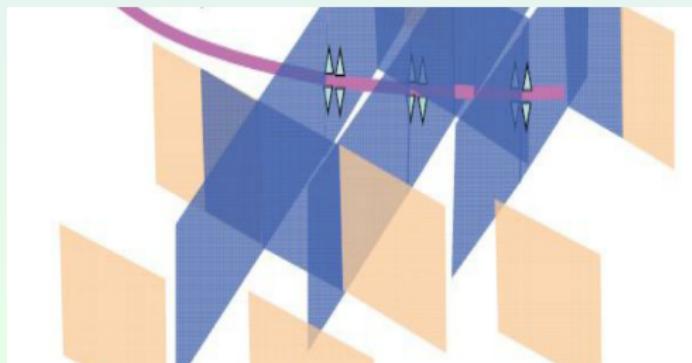
$$\beta_m \frac{\partial P_m}{\partial t} - \nabla \cdot (K_m \nabla P_m) = \textcolor{red}{KI}(P_m - P_c)\delta_\Delta \quad \Omega \subset \mathbb{R}^3$$

$$\beta_f \frac{\partial P_f}{\partial t} - \nabla_\tau \cdot (K_f \nabla_\tau P_f) = (\mathbf{v}_m^+ - \mathbf{v}_m^-) \cdot \mathbf{n} \quad \Gamma \subset \mathbb{R}^2$$

$$\beta_c \frac{\partial P_c}{\partial t} + \frac{dv_c}{ds} = -\frac{\textcolor{red}{KI}}{A_c}(P_r - P_c)$$

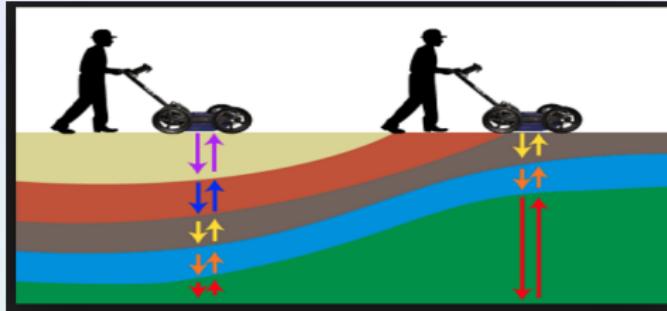
$$v_c = -K_c \frac{dp_c}{ds} \quad \text{in} \quad \gamma_c \quad \mathbb{R}^1$$

δ_Δ – Dirac line source



III Incorporate Outcrop Data

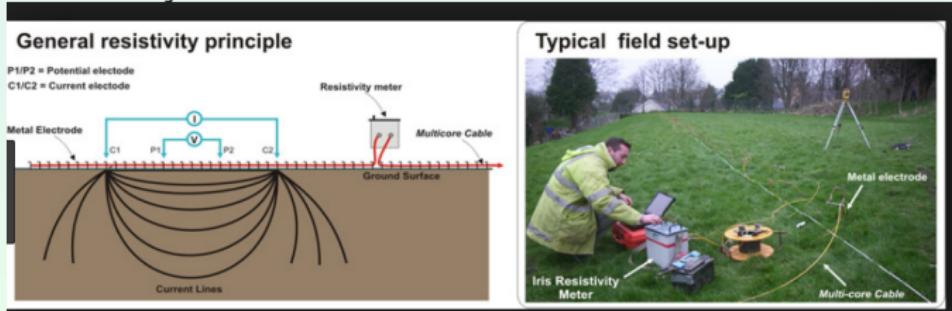
- GPR – Electro-Magnetic Waves



- Near-Surface Seismic Acoustic Waves

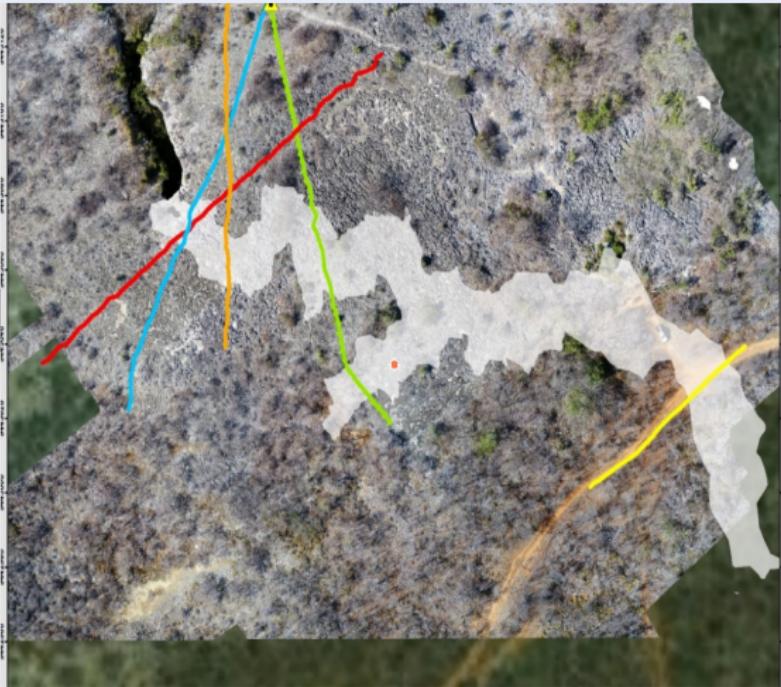


- Electro-Resistivity – Electric Current – Electrodes

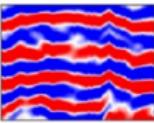
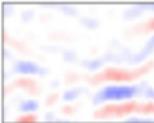
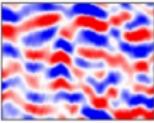


- Joint Work with F Hilario Bezerra and F Pinheiro (UFRN)

Outcrop FURNA FEIA



RADAR FACES

RADARFÁCIES	TIPO DE REFLETOR
R1	
R2	
R3	

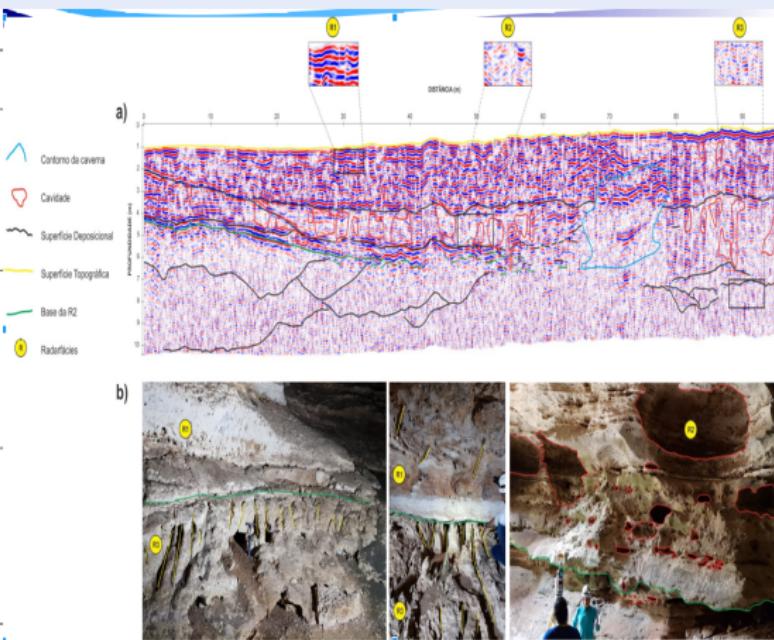
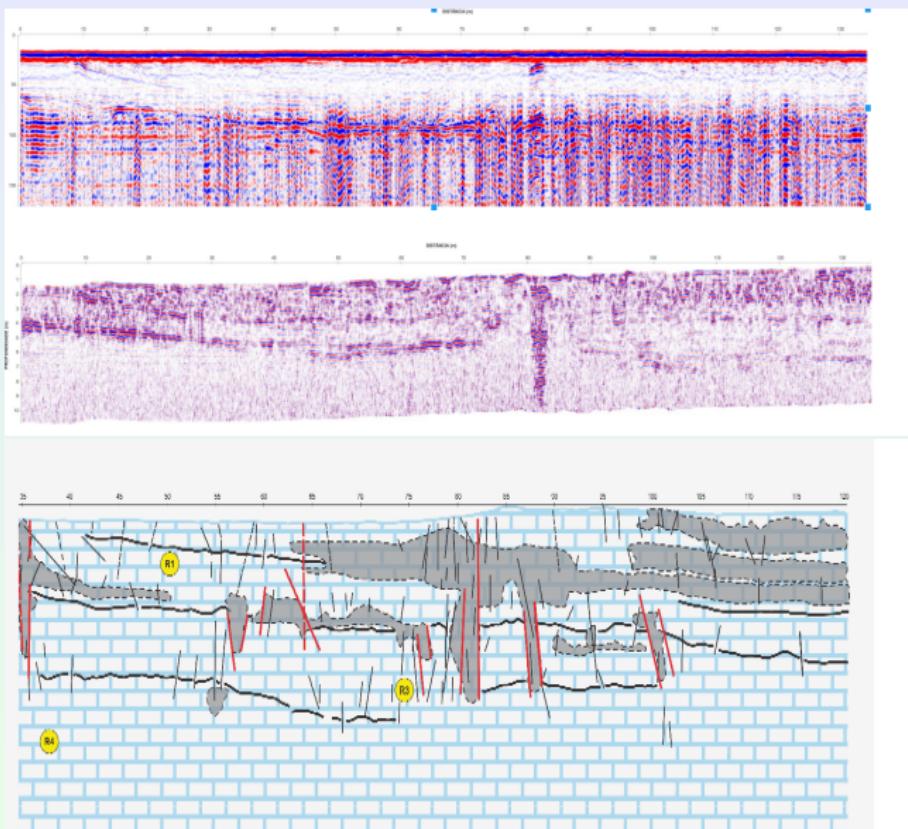
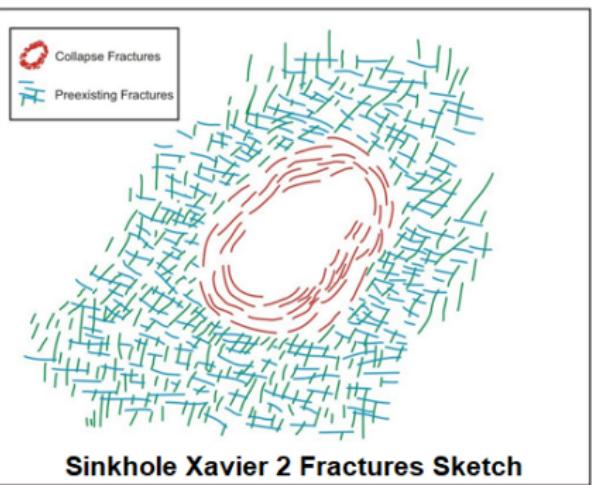
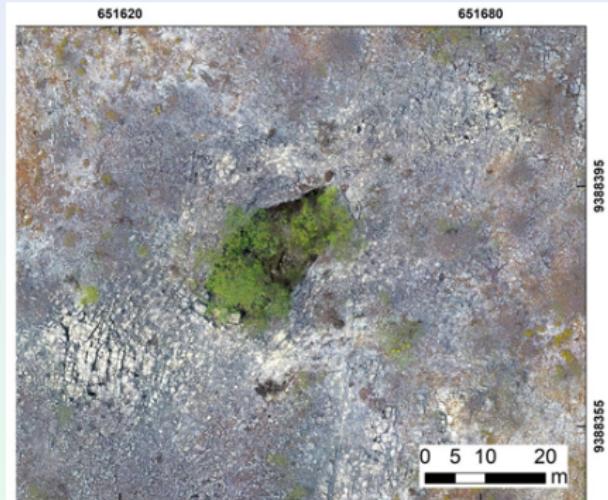


IMAGE PROCESSING



Sinkhole Xavier 2



Sinkhole Xavier 2



Sinkhole Xavier 2 - Materials

Material	Description	Permeability [m ²]
1	Intact Rock	$K_x = K_y = 2.96076 \times 10^{-13}$
2	Intact Rock + Micro fractures (estimated via ODA)	$K_x = 3.07392 \times 10^{-13}$ $K_y = 3.08085 \times 10^{-13}$
3	Intact Rock + Micro fractures (estimated via ODA) + discrete fractures	$K_x = 3.07392 \times 10^{-13}$ $K_y = 3.08085 \times 10^{-13}$
4	Sinkhole	$K_x = K_y = 1.0 \times 10^{-8}$
White Lines	Discrete Fractures	$K_f = 8.333 \times 10^{-10}$ (aperture = 1.0×10^{-4} m)

Estimating ODA:

Micro-Fractures Permeability
 $K_f = 8.333 \times 10^{-10}$ m²

Micro-Fractures Aperture
 $d = 1.0 \times 10^{-4}$ m



Input Parameters: Sinkhole Xavier 2

Parameters	Values
Domain	$500\text{m} \times 500\text{m}$
Rock Permeability (Horizontal)	$K_x = 3.2433 \times 10^{-13} \text{ m}^2$
Rock Permeability (Vertical)	$K_y = 3.2815 \times 10^{-13} \text{ m}^2$
Initial Pressure	56 MPa
Well Pressure	55 MPa
Sinkhole Pressure	55 MPa
Karst Index	$7.370811 \times 10^{-13} \text{ m}^3$
Total Simulation Time	$4 \times 10^5 \text{ s}$
Time Step	2000 s

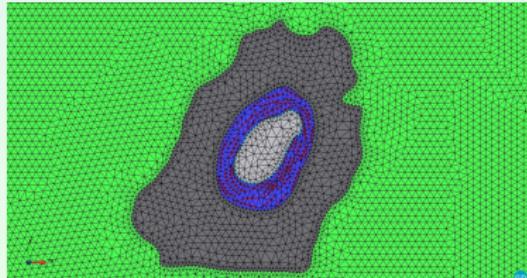
Sinkhole Xavier 2

Two simulations were performed:

- High Fidelity Simulation
- Macro Scale Simulation using Karst Index

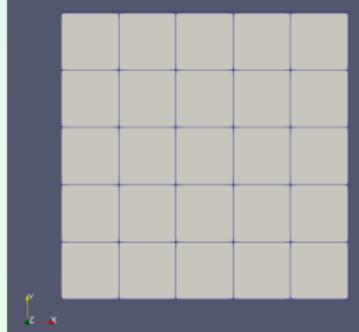
Simulation	High Fidelity	Macro Scale
Number of Elements	578412 (triang.)	25 (quad.)
Number of Nodes	290107	36
Processing time	7 minutes	1.42 seconds

High Fidelity Mesh (zoom)



(LNCC)

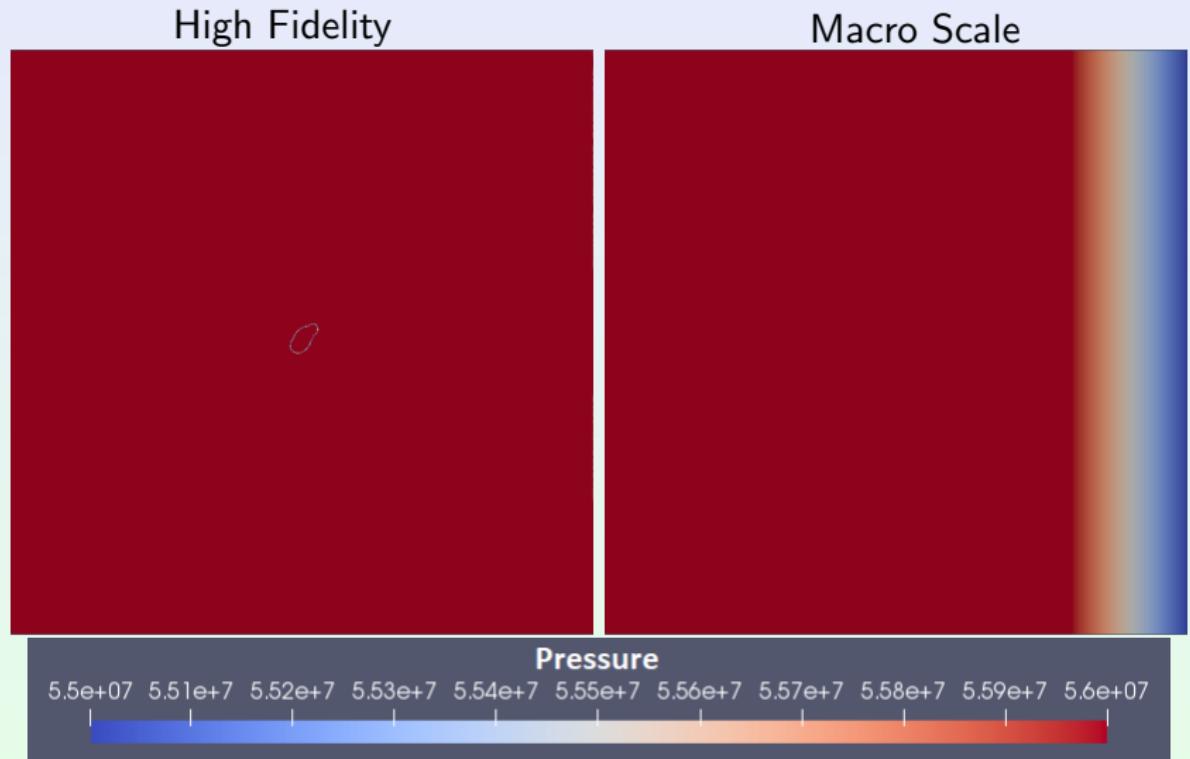
Macro Scale Mesh



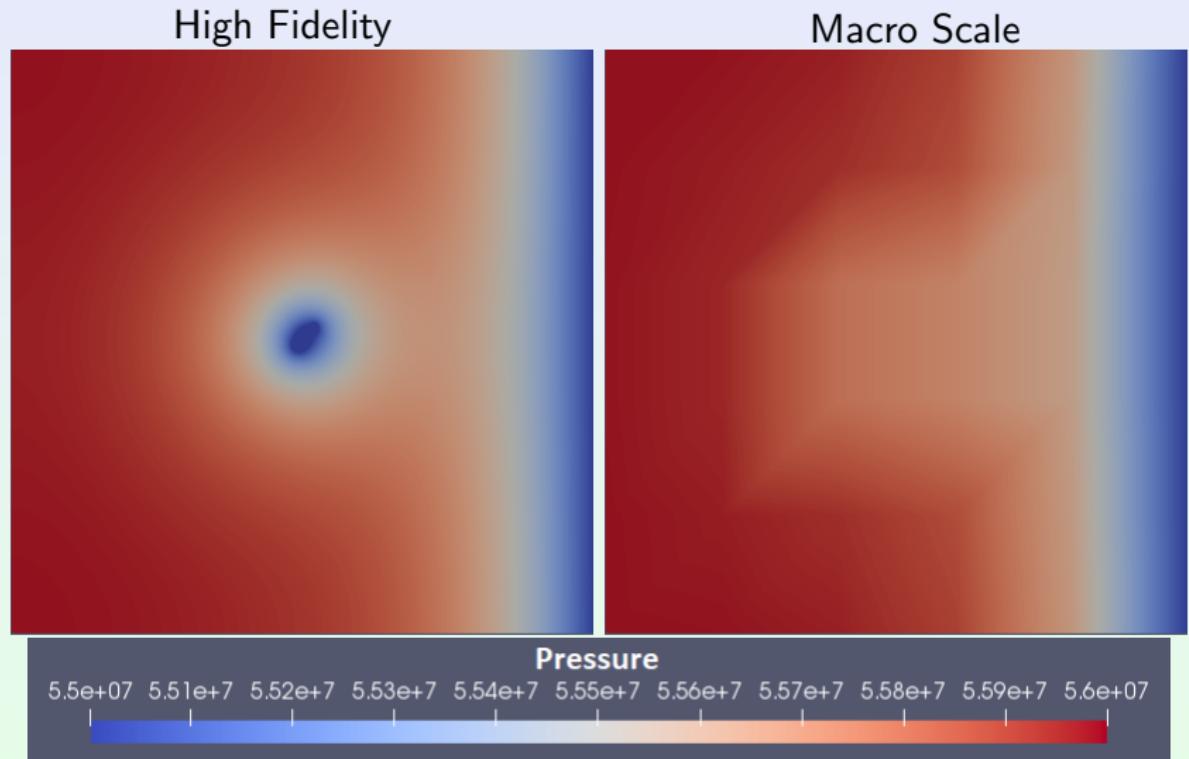
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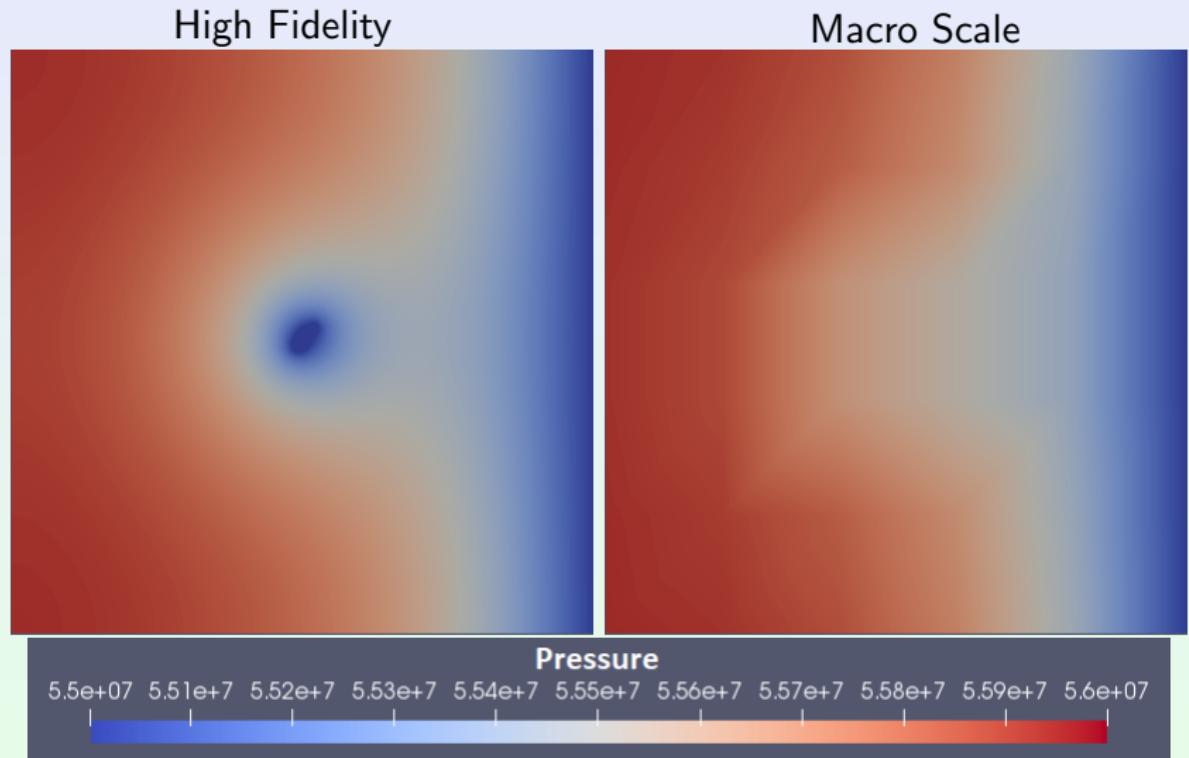
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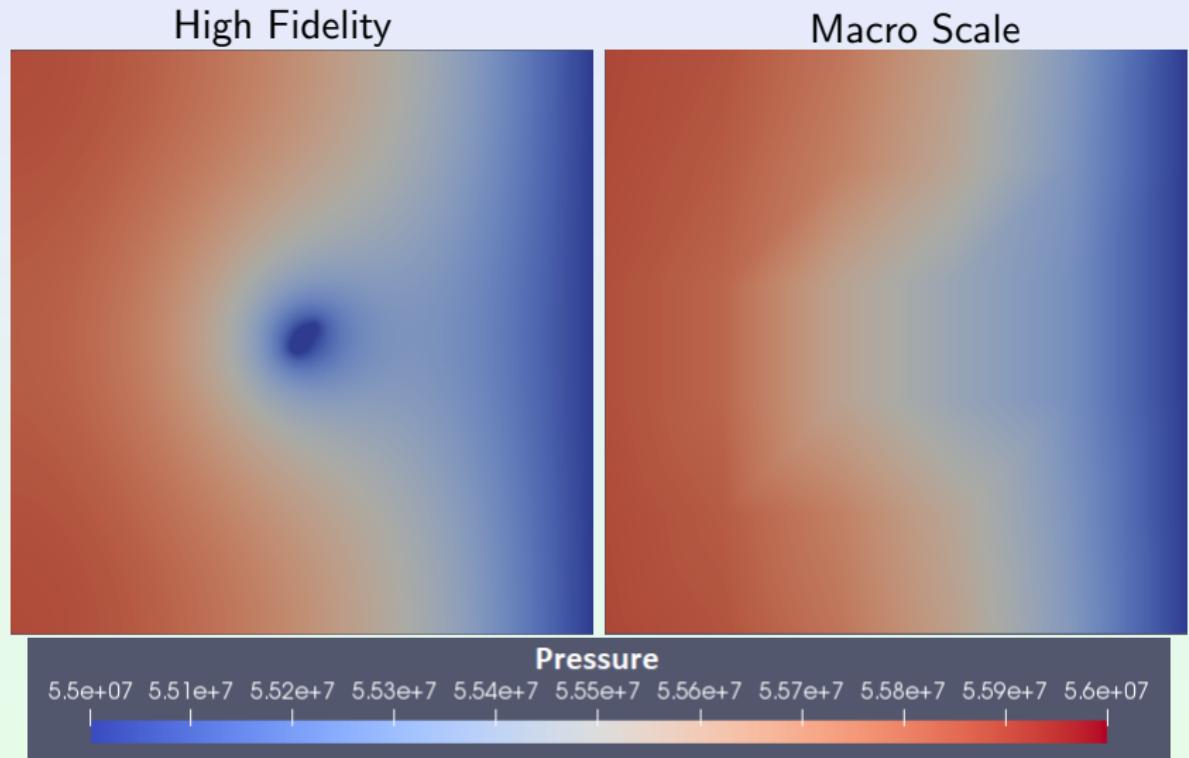
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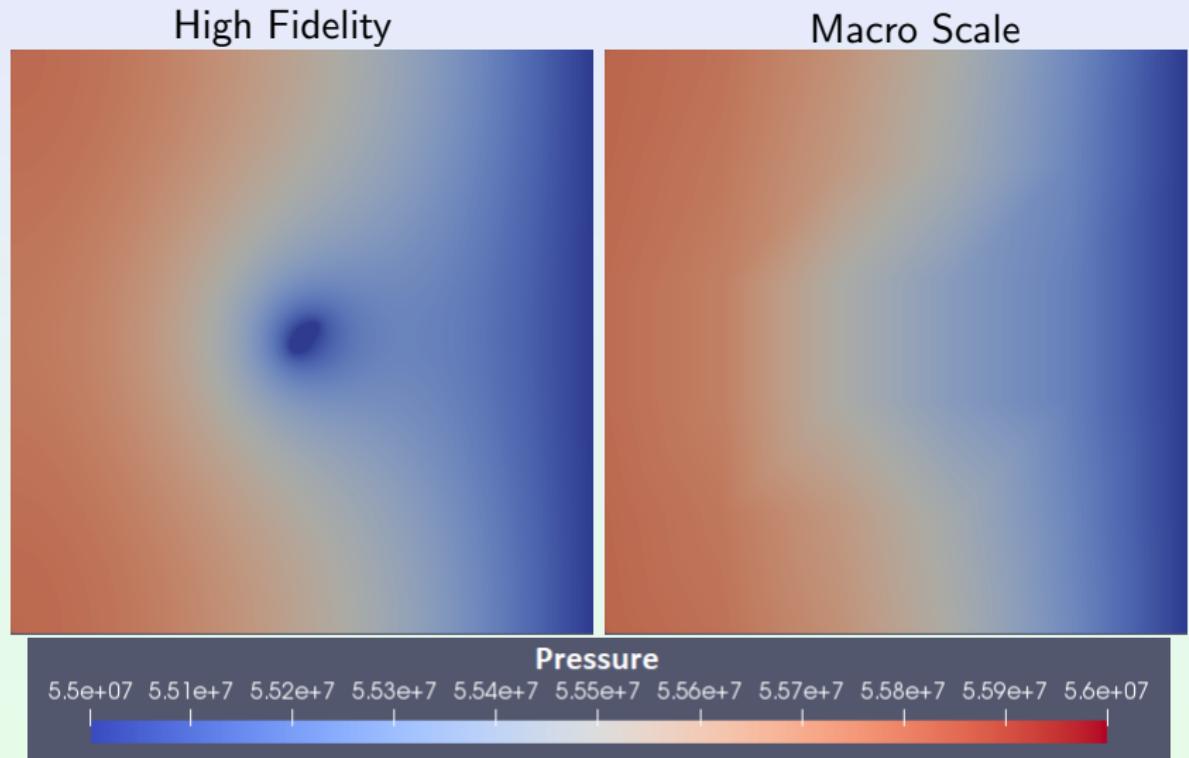
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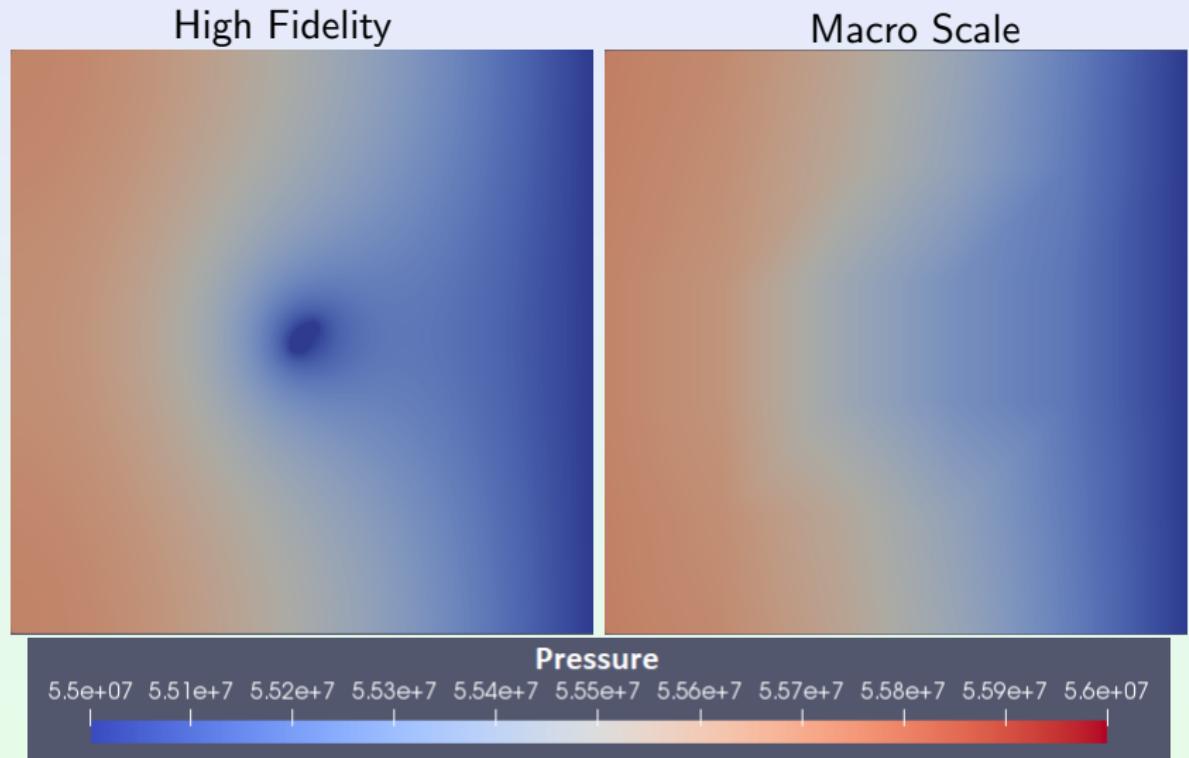
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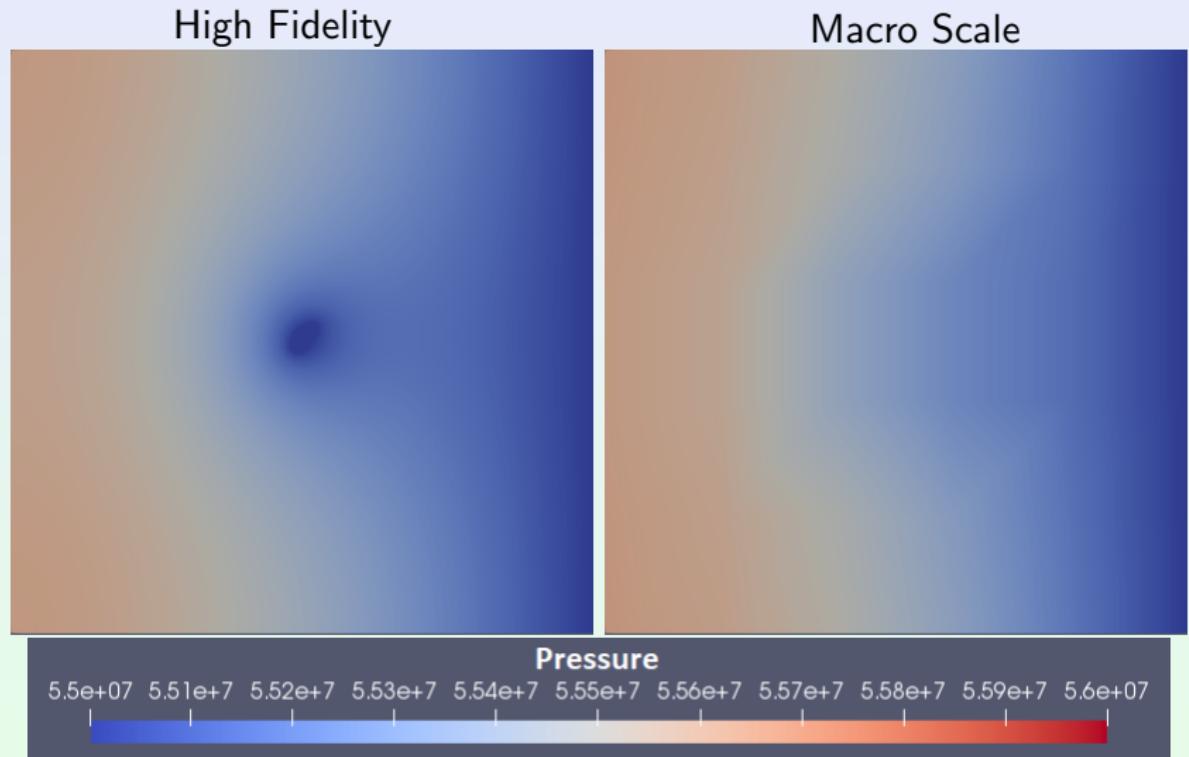
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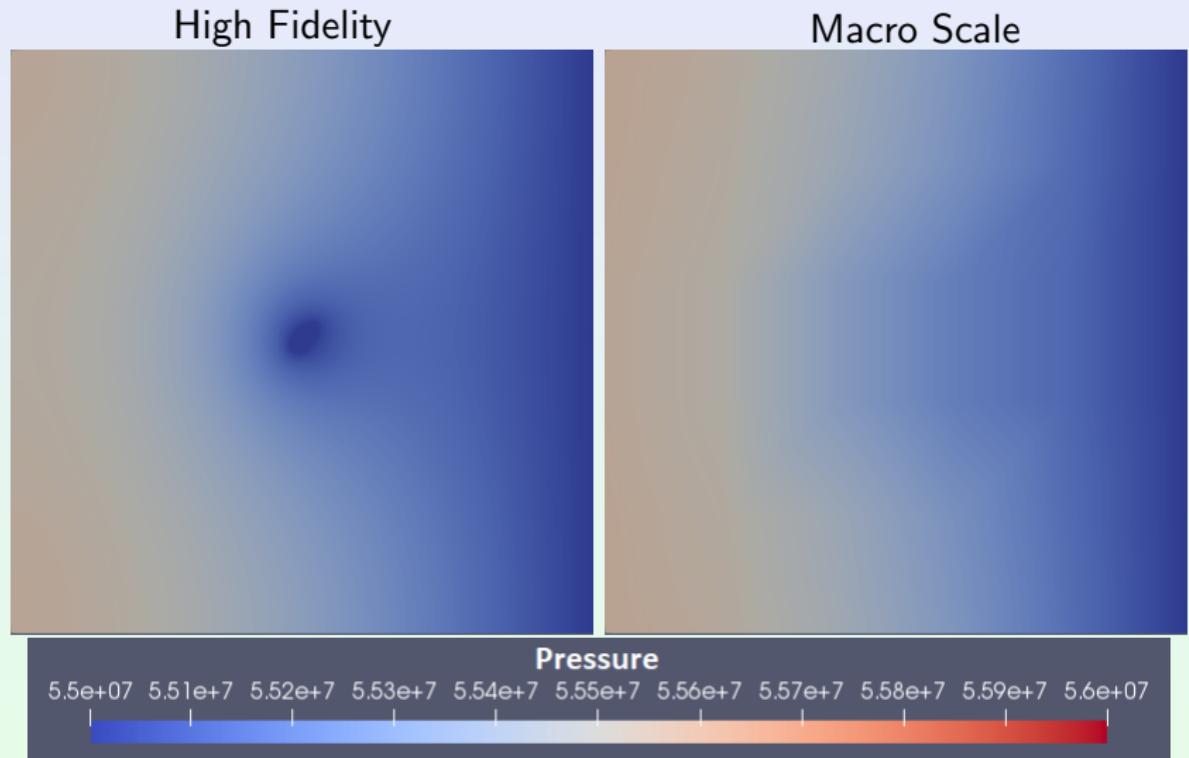
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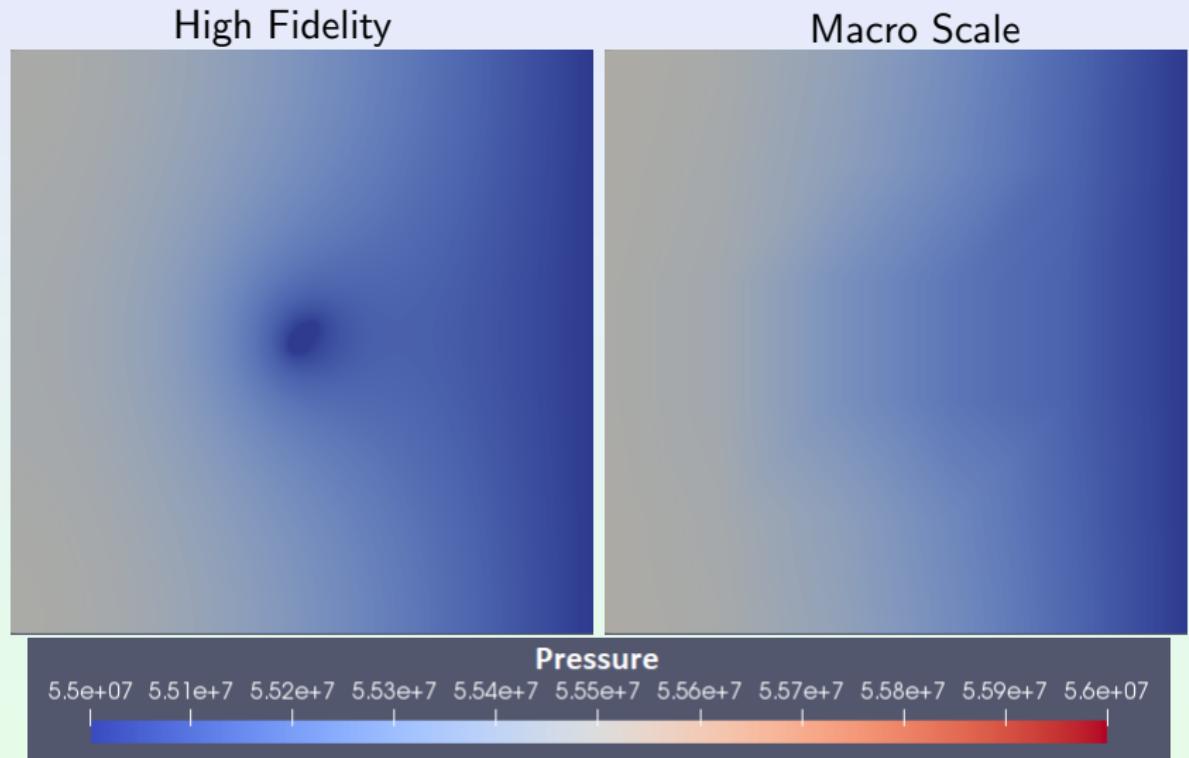
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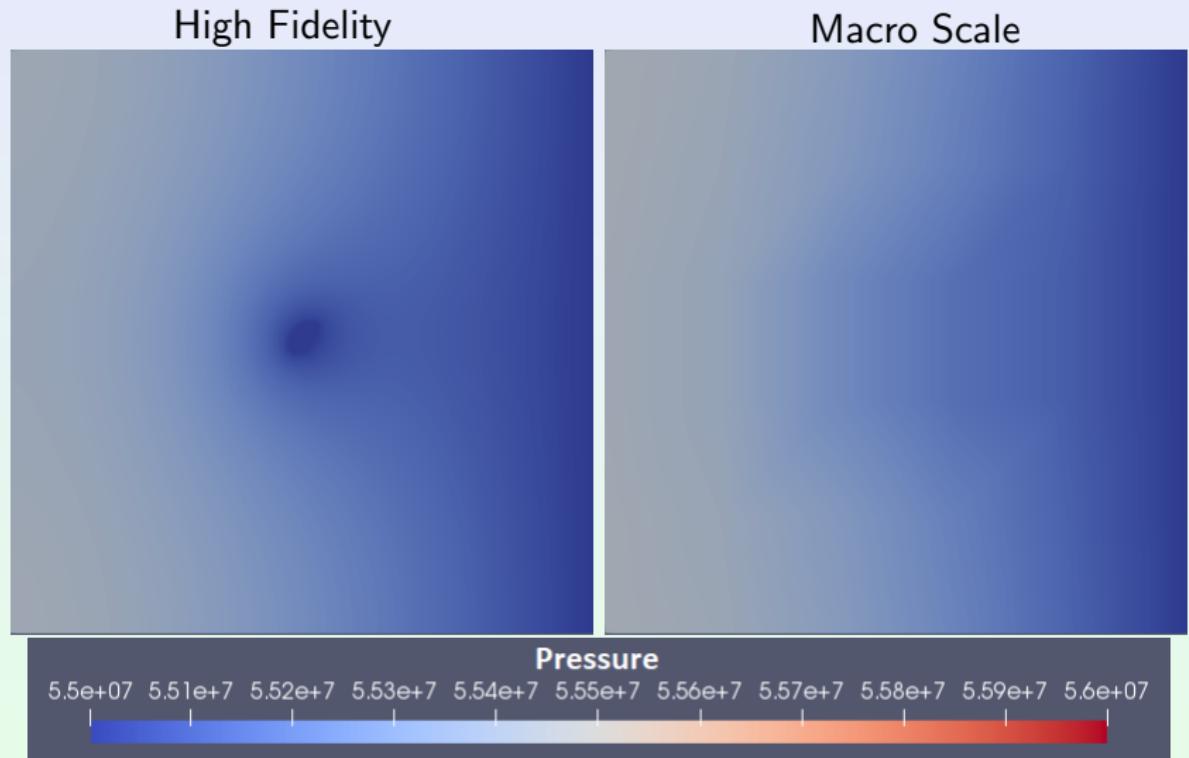
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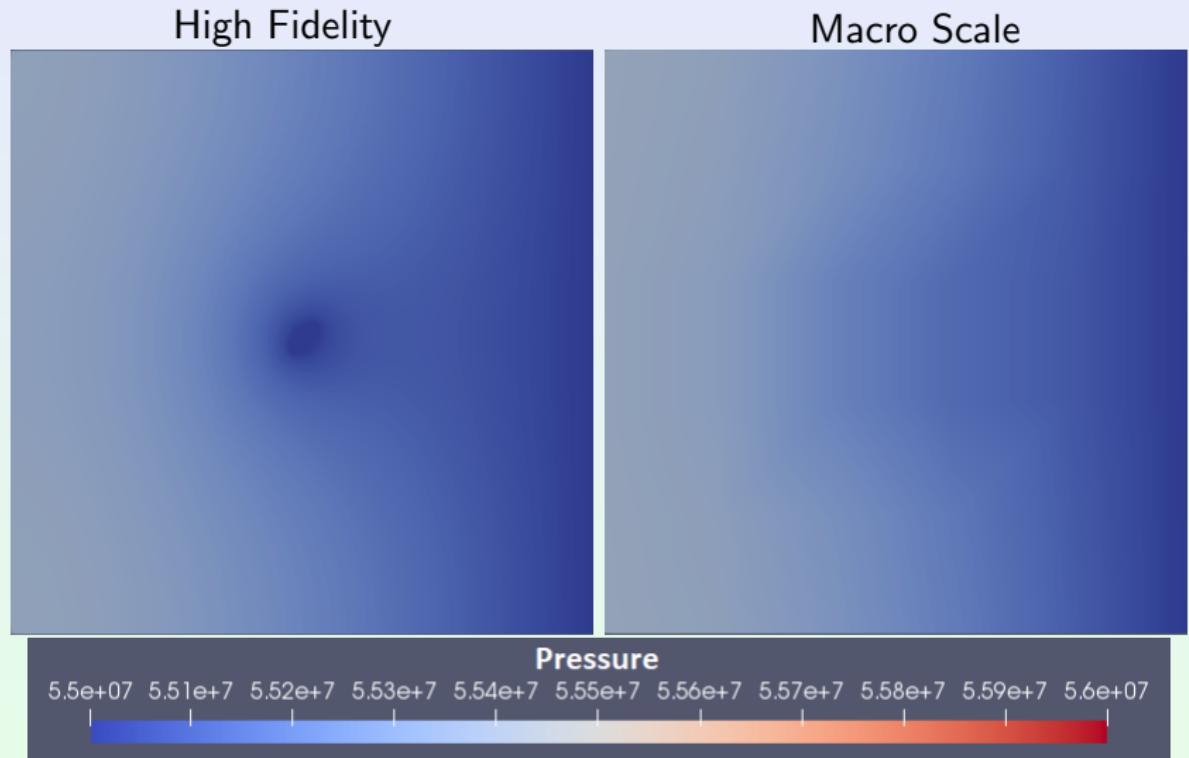
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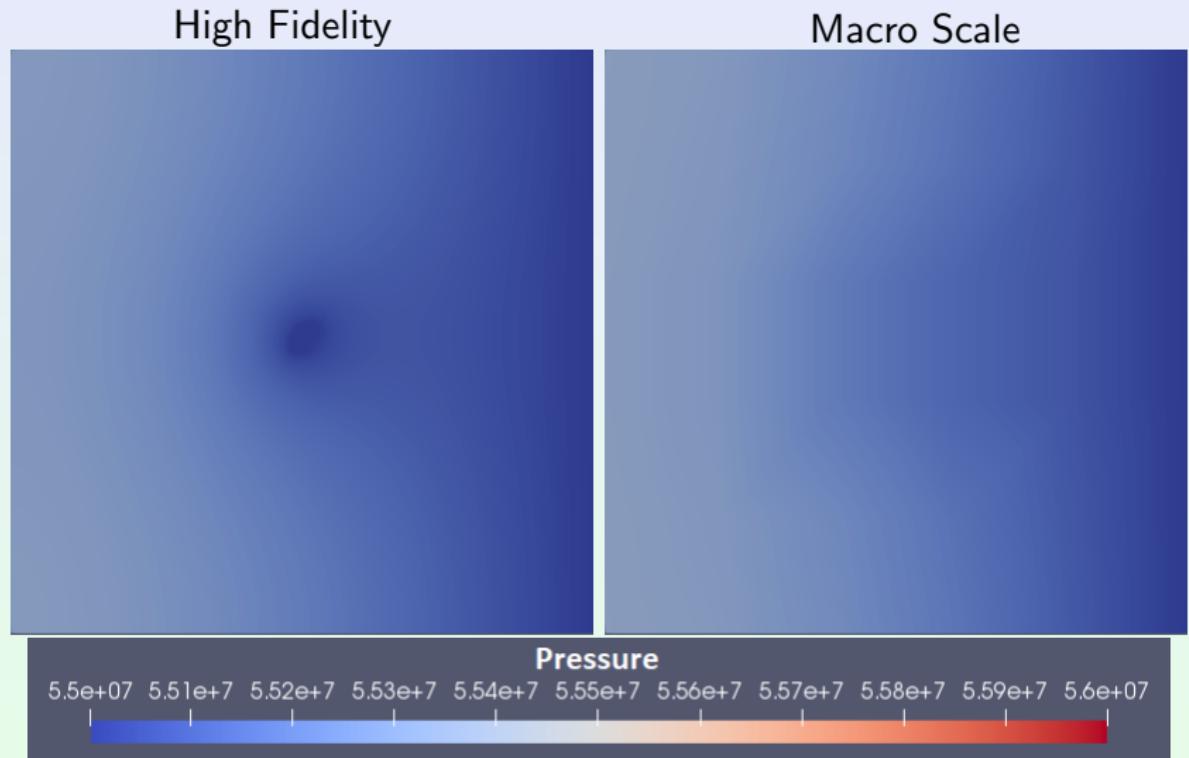
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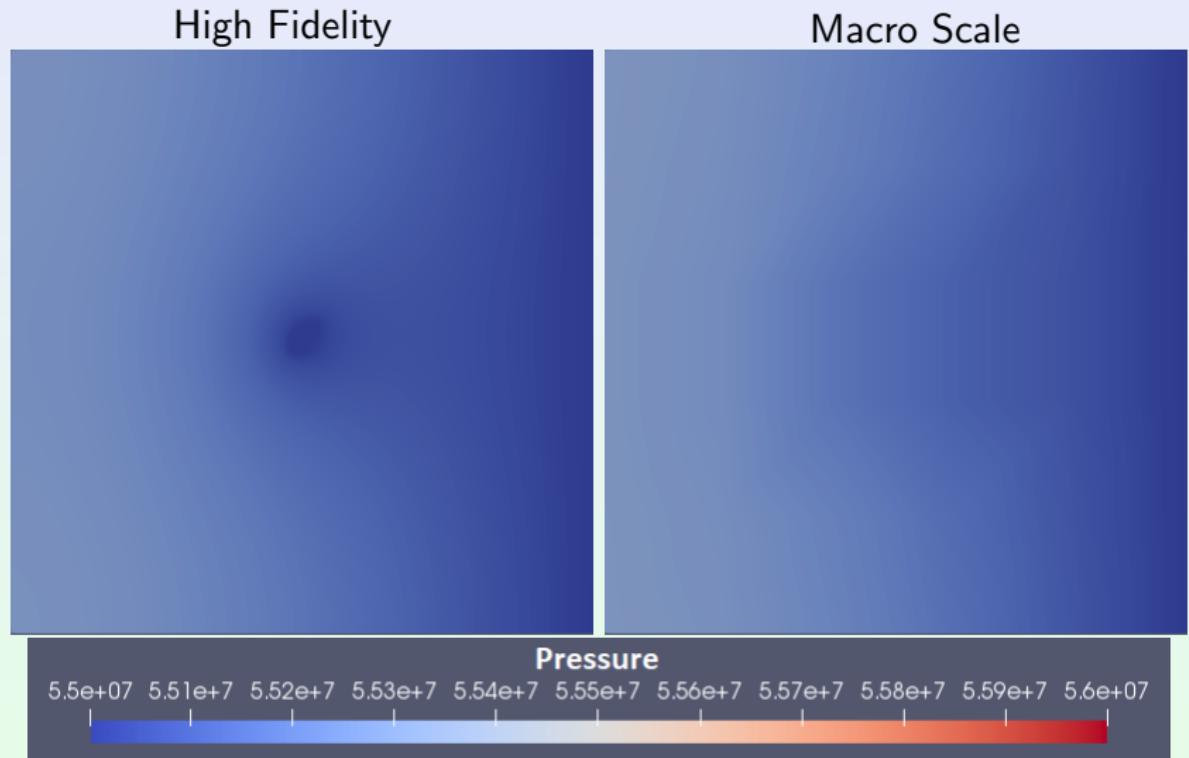
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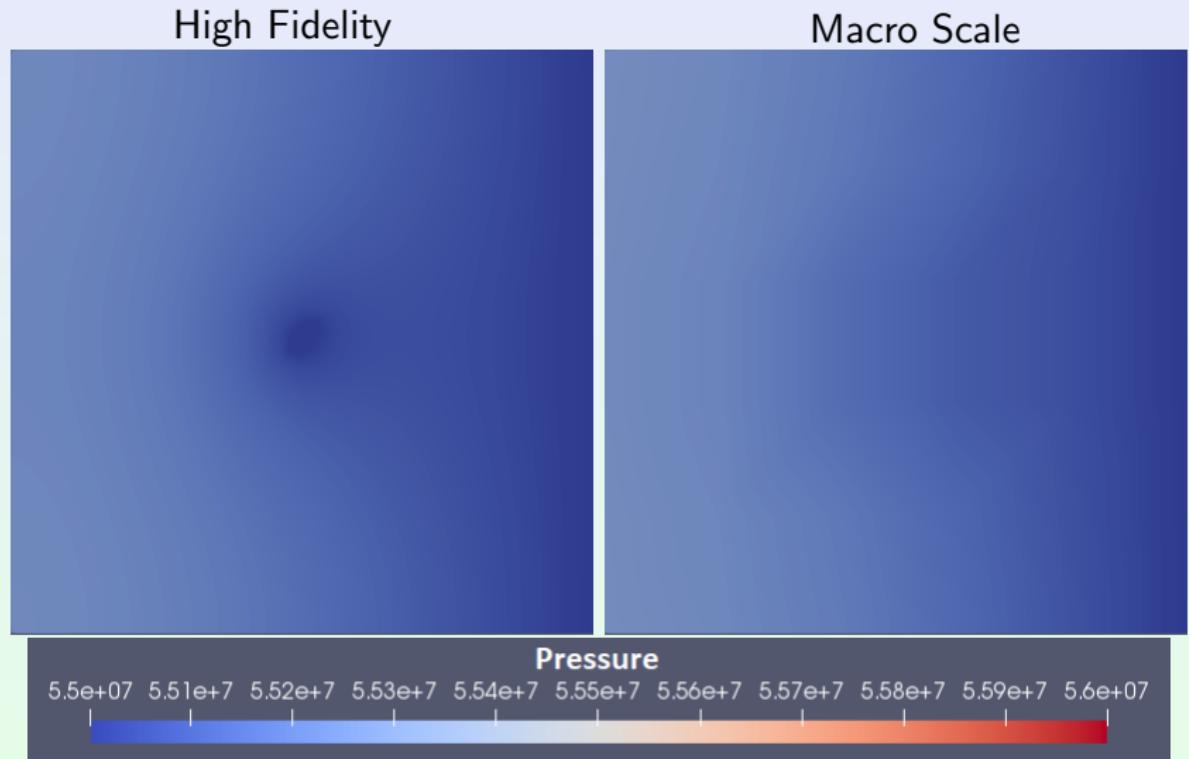
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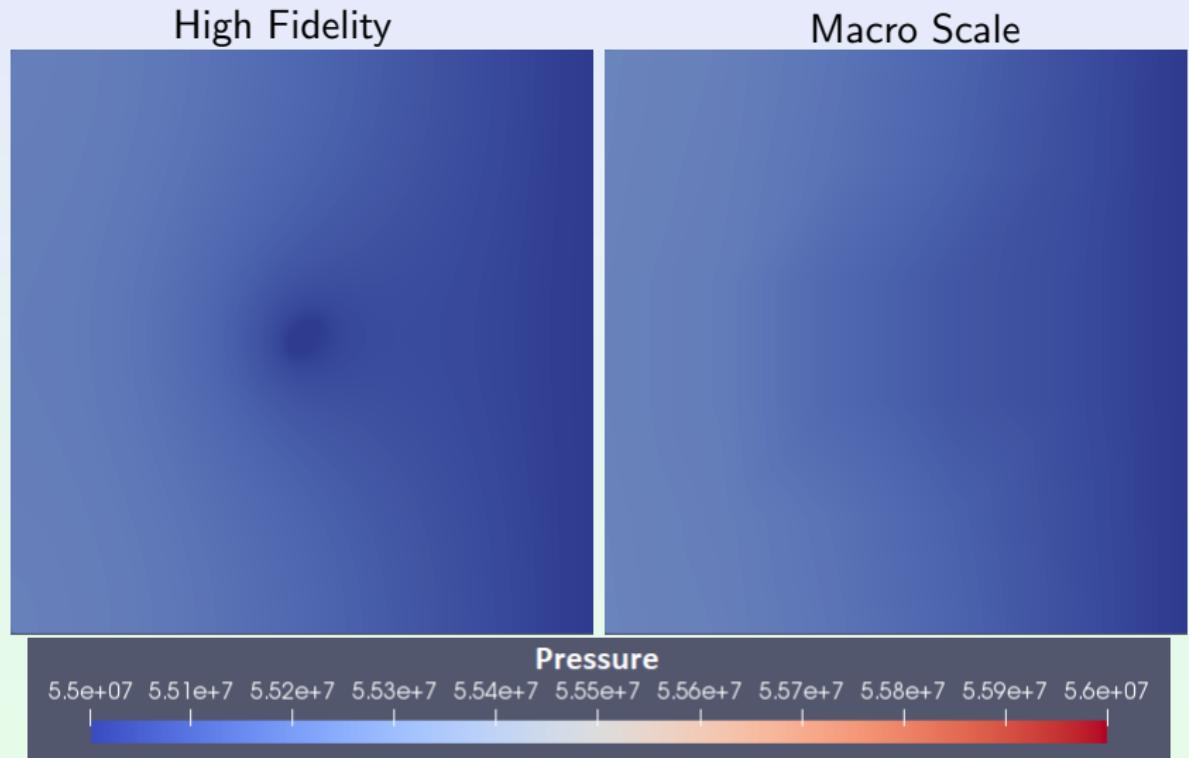
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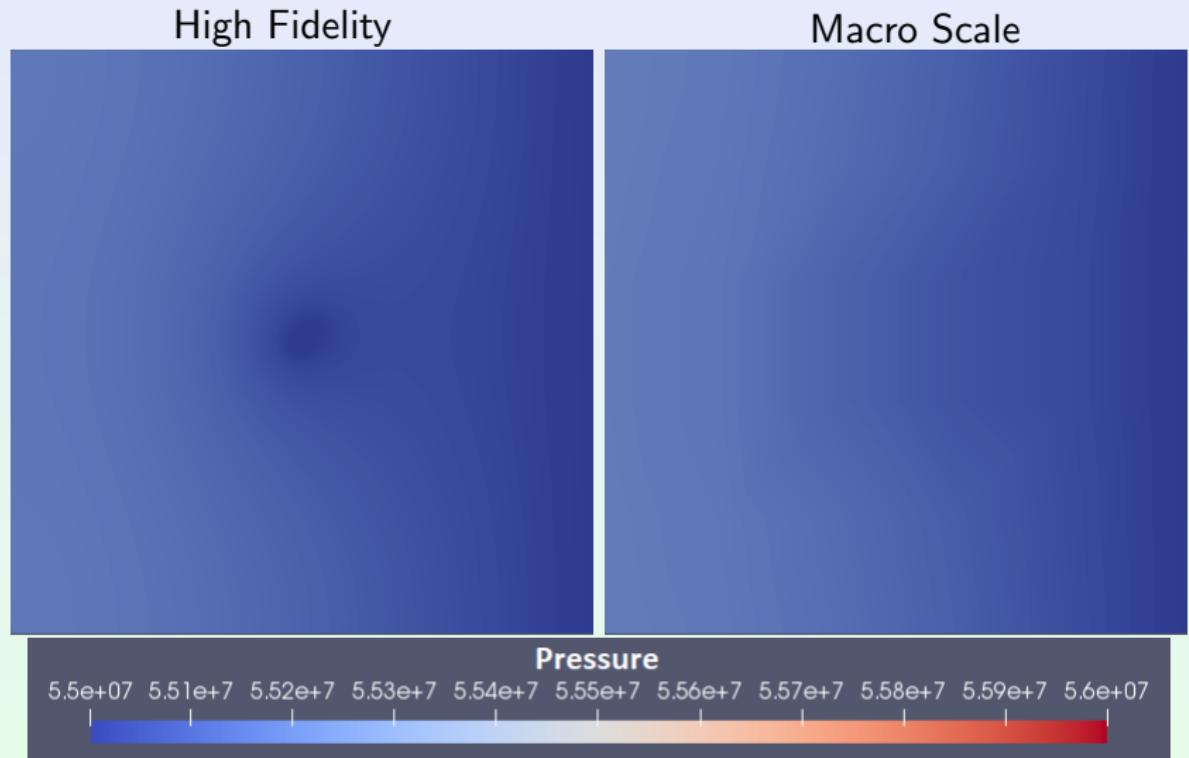
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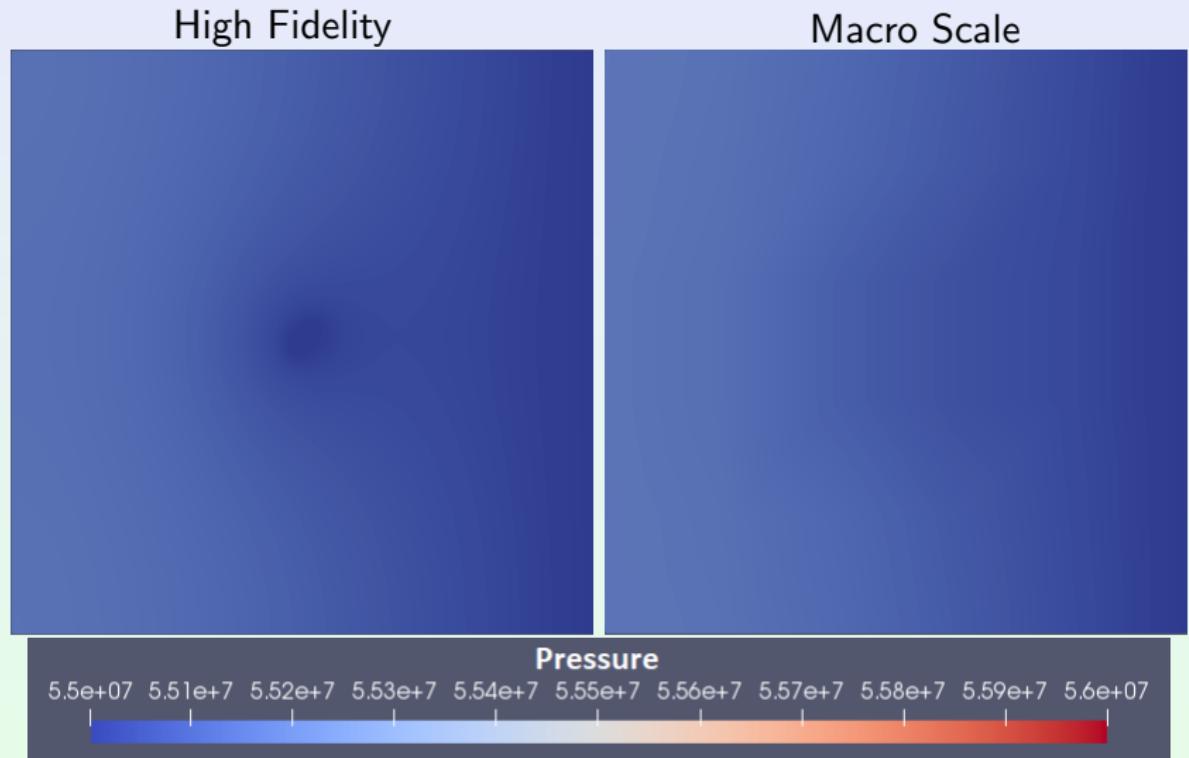
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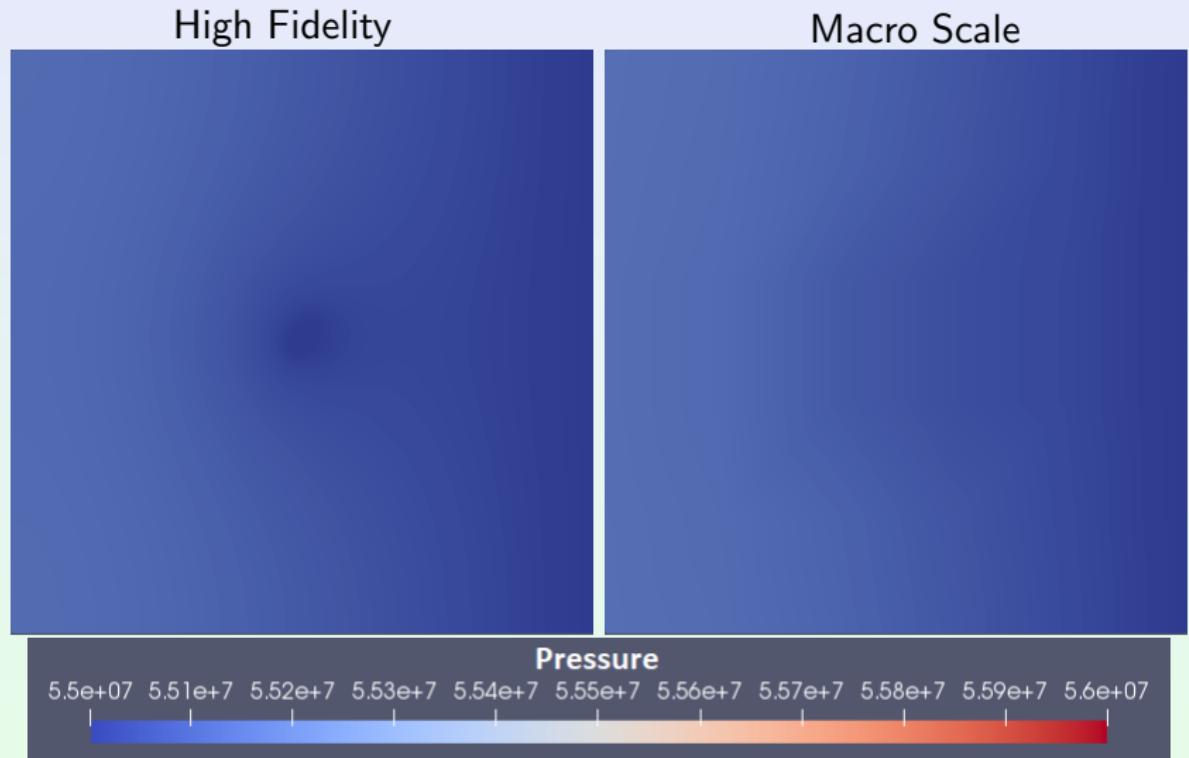
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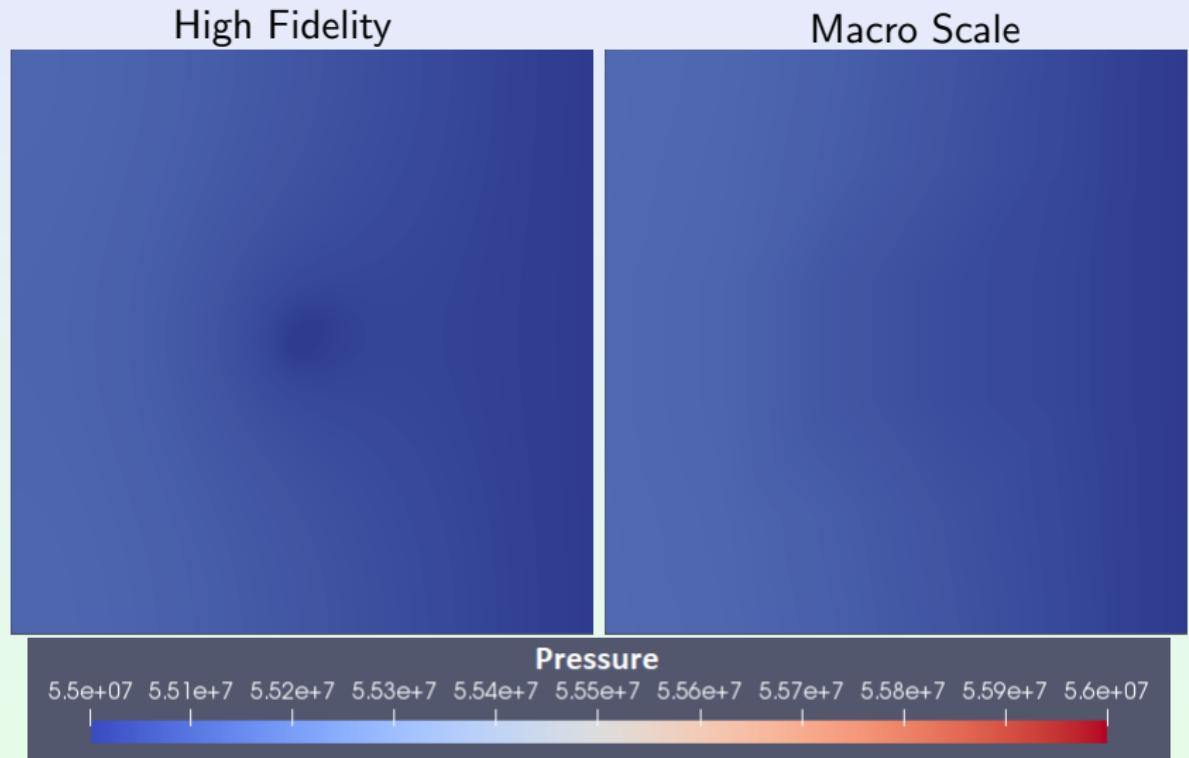
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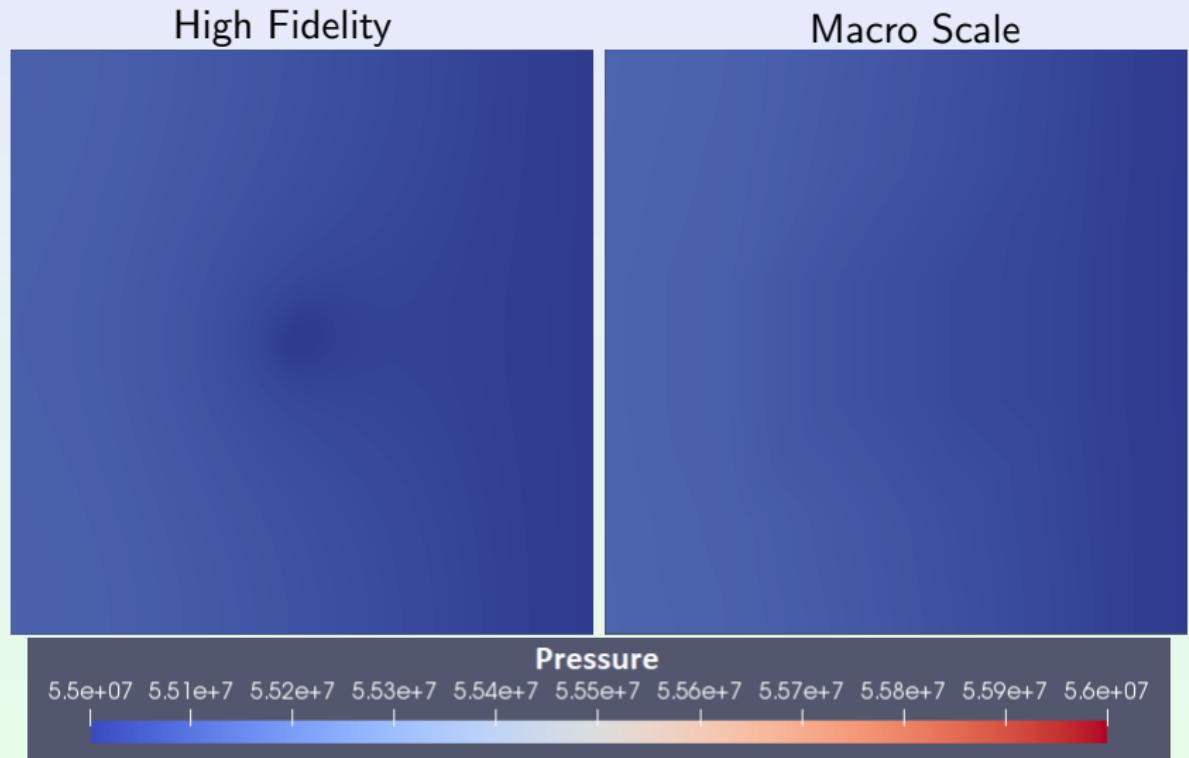
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Sinkhole Xavier 2



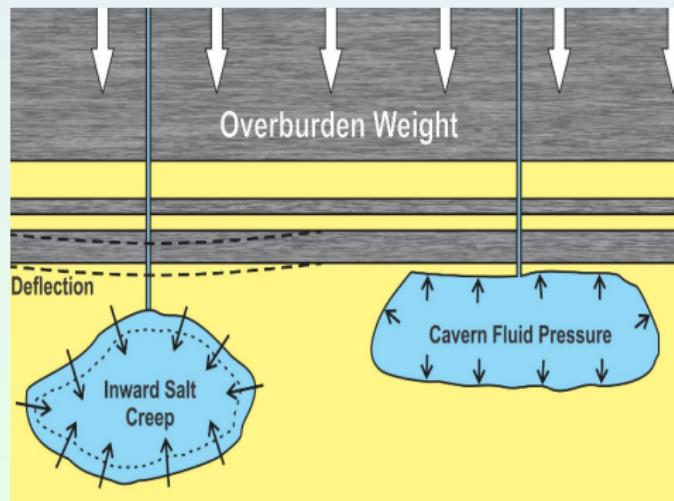
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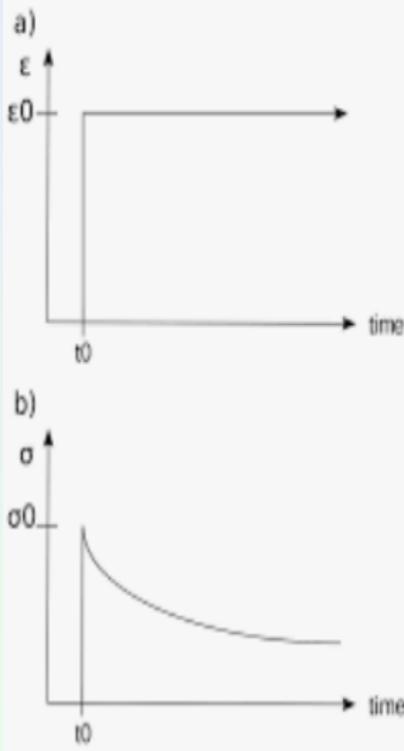
Storage in Salt Dome Caverns

Efficient underground repository

- Inject Fresh Water; withdraw brine dissolving the salt
- Create a stable large Cavity. Salt is chemically inert to CO_2
- Also potential sites for energy storage using highly compressible gases
- **Creep.** Salt tends to fill the holes gradually moving towards the cavern

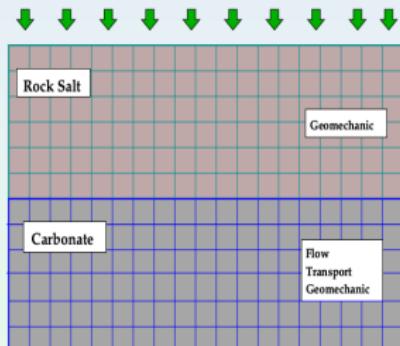
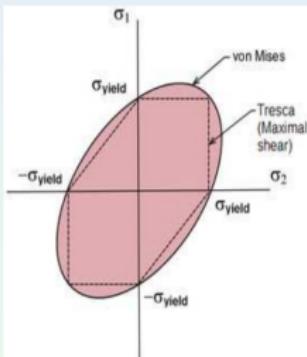


Creep Model for Halite



Geomechanics: Von Mises Stress – Distortional Energy

$$\sigma = -p\mathbf{I} + \mathbf{s}, \quad Q = \sqrt{\frac{3}{2} s_{ij} s_{ji}} \quad \frac{\partial \mathcal{E}_c}{\partial t} = \epsilon_0 \left(\frac{Q}{\sigma_0} \right)^N \sqrt{\frac{3}{2} \|\mathbf{s}\|}$$



Viscoelastic Model for the Rock Salt

Q – Energy that triggers creep in the saline cap rock

CONCLUDING REMARKS

- Great Opportunity for CO_2 -storage in Pre-Salt
- Salt Layer
 - Self-Healing due to Creep
 - Chemically Inert to CO_2
 - Impermeable Geological Formation

Energy: WAG – Water Alternate Gas Injection for Oil Recovery

